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AFTERBODY DRAG
VOLUME 1 - DRAG OF CONICAL AND CIRCULAR
ARC AFTERBODIES WITHOUT JET FLOW
by

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NOTATION

A	Area
A_j	Jet exit area
A_m	Maximum cross-sectional area
$C_{D\beta}$	Pressure drag coefficient of a boattail = D_β/qA_m
C_{P_b}	Base pressure coefficient = $\frac{P_b - P_\infty}{q}$
d_b	Base diameter
d_j	Jet exit diameter
d_m	Maximum diameter
P_b	Base pressure
P_∞	Free-stream static pressure
q	Free-stream dynamic pressure
β	Terminal angle of boattail

ABSTRACT

The results of the afterbody drag study are presented in four volumes--Volume 1: Drag of Conical and Circular Arc Afterbodies; Volume 2: Jet Interference Effects on Subsonic Boattail Drag; Volume 3: Literature Survey; and Volume 4: Data and Analysis.

Volume 1 includes a series of charts that enable the drag of conical and circular arc afterbodies without jet flow to be determined.

ADMINISTRATIVE INFORMATION

The work reported was performed for the David W. Taylor Naval Ship Research and Development Center by Payne, Incorporated under ONR Contract N00014-77-C-0039 as part of an evaluation of afterbody drag. The afterbody drag project was supported by the Naval Air Systems Command and the Naval Weapons Center under Program Elements 63361N, 62332N, and 52241N; Task Areas W15X20000, F32.322.203, and WF41.421.201; and Work Units 1660-234 and 1660-235.

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INTRODUCTION

Aerodynamic drag is one of the major factors to be considered when attempting to predict airborne vehicle performance. Although there are sources of aerodynamic drag, such as wings, fuselage, nose, and tails, the afterbody drag of the fuselage is usually the most difficult to evaluate. Inasmuch as some vehicles develop 30 percent of their zero-lift drag from the afterbody, an accurate method for predicting the magnitude of this drag is needed.

Afterbodies as a rule are tapered, or boattailed, in some manner. These afterbodies suffer from skin friction drag, base drag, and pressure drag. As air flows over the junction of the forebody and the boattail, a low pressure peak is developed. As the flow continues downstream the pressure rises, depending upon the boattail length and curvature. In some cases the pressure can exceed that of the free stream. For most practical shapes, however, the pressure distribution over the boattail results in a pressure drag. Even though the tapered afterbody develops a pressure drag,

its overall effect is less total afterbody drag. This is because the taper both reduces the base area and increases the pressure on the aft-facing base such that the base drag is appreciably reduced.

The results of the afterbody drag study performed at DTNSRDC are presented in four volumes:

Volume 1 - Drag of Conical and Circular Arc Afterbodies without Jet Flow

Volume 2 - Jet Interference Effects on Subsonic Boattail Drag

Volume 3 - Literature Survey

Volume 4 - Data and Analysis

The objective of the phase of the study presented in Volume 1 is to establish a data base of afterbody drag charts based on data from the numerous references (608) listed in Volume 3.

STATE OF THE ART

A survey of the afterbody drag literature disclosed that the vast majority of available reports on experiments related to the subject were quite specialized, treating nonbasic specific configurations, and were not suitable for establishing a broad basis from which the effects of the various geometrical, physical, and environmental parameters could be systematically investigated. Only a small number of reports were suitable for this purpose. The widest range of useful reports were for conical afterbodies in the subsonic and transonic range; however, a number of reports on systematic investigations of nonconical afterbodies (such as circular arc) were also useful.

The surveyed reports are in three groups: (1) experimental data, (2) empirical and semiempirical methods of correlation, and (3) theoretical models of the flow. Only a small number of reports in the first group were suitable for the correlation of boattail drag and base pressure coefficients as a function of the geometric parameters of the boattail. Those reports most valuable were References 1 through 10.* In the second group, four different approaches were considered. These approaches were proposed in References 11, 12 and 13, 14 and 15, and 16.

*A complete listing of references is given on page 51.

McDonald and Hughes¹¹ proposed a method for a correlative prediction of boattail and base drag of parabolic, circular arc, and conical afterbodies including the effect of jet flow on the drag characteristics of the three types of afterbodies. However, the method does not consider variation of the drag characteristics with Mach number. The variation with Mach number, even in the subsonic range from Mach number 0.6 to 0.9, can be considerable. There are also other restrictions in the use of the method. McDonald and Hughes¹¹ base their correlation method on the finding that there is a unique relationship between the base pressure and the boattail drag, and that this relationship is essentially linear over the greater part of the base pressure range. This finding appears to be confirmed by Kurn.⁸ Furthermore, McDonald and Hughes¹¹ found that if the three afterbody shapes have identical afterbody angles β at the base and identical base diameter ratios d_b/d_m , the boattail drag coefficients are approximately the same, and the base pressure coefficients are approximately the same for the circular arc and the parabola.

According to the present investigation, the McDonald and Hughes¹¹ finding in regard to the boattail drag appears to be confirmed in the Mach number range from 0.6 to 0.8, considering the uncertainties of the data. However, for Mach numbers of 0.9 and higher, the boattail drag curves for conical and circular arc afterbodies in the present investigation appear to be quite different.

Bergman¹² presents a qualitative and quantitative analysis of the effect of nozzle geometry and some physical parameters on the boattail drag. However, base drag and the effect of Mach number are not considered. A subsequently proposed method by Kurn⁸ also does not consider base drag and is suggested only for Mach numbers less than 0.9. The latter approach corrects a "basic drag," which is a boattail drag with a cylindrical sting, for the jet effects of the actual plume shape and the entrainment. The advantage of this approach is that if the basic drag of the boattail with a cylindrical sting can be evaluated with sufficient accuracy on a parametric basis, the corrections for the plume shape and entrainment effects may be significantly smaller than in the no-sting case. The method is applicable in the jet-on case for afterbodies with no base area.

The method of Swavely and Soileau¹⁴ uses a parameter IMS (Integral Mean Slope) which is obtained by integrating an area ratio equation:

$$IMS = \frac{\int_{(A_j/A_m)}^{1.0} \frac{d(A/A_m)}{d(X/d_{eq})} d(A/A_m)}{1 - (A_j/A_m)}$$

where

$$d_{eq} = \left(\frac{4 A_m}{\pi} \right)^{1/2}$$

Thus, the parameter IMS is obtained from the boattail and nozzle geometry as a function of the area ratios and the axial coordinate from the maximum cross-sectional area point aft. The method was designed for arbitrary and complex afterbody shapes including twin jets. However, as shown by Brazier and Ball,¹⁵ the method failed for configurations whose area plots involved regions of steep slopes aft of the point where separation occurs. To correct this problem, an IMS_T (Integral Mean Slope-Truncated) approach was introduced. This approach is based on specifying a maximum slope of the nondimensional area distribution which can be used in the IMS calculation. The specified maximum slope is substituted for the real slope at each step of the IMS calculation for which the real slope exceeds the maximum. Even with this improvement, Brazier and Ball¹⁵ urge extreme caution in predicting nozzle and afterbody drag from data obtained with a "representative" forebody to a forebody of arbitrary shape and length; see Effect of Reynolds Number, page 11. The method apparently is applicable to subsonic flight and is limited to configurations with negligible annular base area.

The prediction method of Presz and Pitkin,¹⁶ which is applicable to the subsonic case, requires extensive computations. The method predicts

the flow separation point and pressure distribution on a boattail with a given solid surface sting in subsonic flow. After determination of the flow separation point, an iterative method is used to match a calculated inviscid flow field, an attached boundary layer, a control volume separation point, and the separated flow field model. The pressure distribution obtained then may be integrated to give the boattail pressure drag coefficient. The method does not consider base drag and effects of jet plume shape and entrainment.

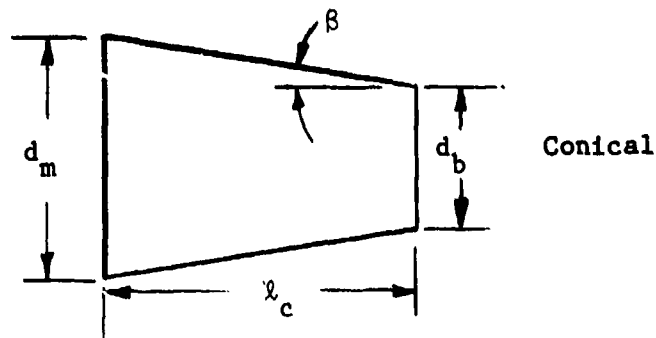
The four methods presented are considered to be representative of the approaches proposed for the solution of the afterbody drag prediction problem in the subsonic and transonic range. The methods, as reported in the references, show correlations for some specific conditions, boattail configurations, and Mach numbers. The prediction reliability for other conditions, configurations, and Mach numbers has not been estimated.

With respect to supersonic afterbody drag, theory is of greater applicability because supersonic flow is easier to treat mathematically. Consequently, a number of mathematical treatments of afterbody drag in supersonic flow are available. Although the supersonic case beyond $M = 1.3$ was not considered in this investigation, the work of Chapman,¹⁷ with respect to base pressure, is fundamental. A correlation based on the Chapman method for a variety of configurations and local Mach numbers is discussed by Love.¹⁸ The base pressure is also useful in determining the boattail drag coefficient in the supersonic case. A substantial amount of material is available to allow a systematic treatment of boattail and base drag.¹⁹⁻²² An evaluation of the methods presented in References 19 through 22 has been made by King.²³

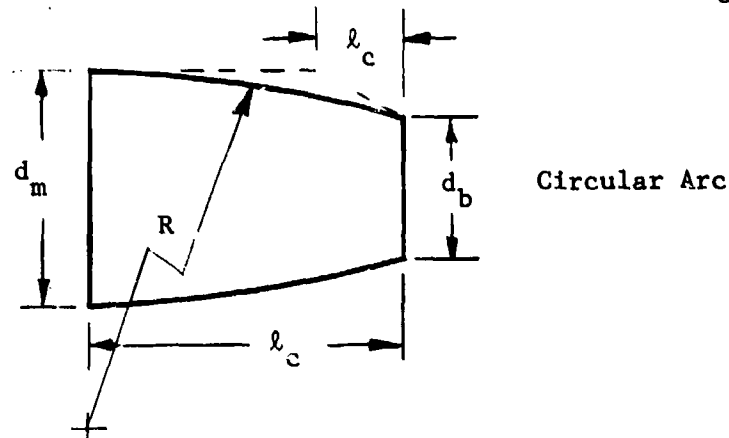
DISCUSSION

AFTERBODY GEOMETRY

A conical boattail is completely defined by the boattail angle β and the diameter ratio d_b/d_m :



A nonconical afterbody may involve any kind of curvature of the boattail. The number of parameters defining these boattails is generally larger than two, unless the forebody is tangent to a circular arc afterbody. McDonald and Hughes¹¹ and Reid and Hastings²⁴ indicate that the most important parameter besides the diameter ratio is the boattail angle at the base - β .



The relationship among the parameters β , d_b/d_m , and l/d_m is shown in Figure 1 for conical afterbodies and in Figure 2 for the circular arc afterbodies.

DRAG OF CONICAL AFTERBODIES

Boattail Drag

Experimental data used for correlation of conical boattail drag shown in Figure 3 were taken from References 1 and 2. Data from other sources were also considered, but are not included in this correlation. The no-jet flow experimental data of Cubbage¹ displayed a very systematic, consistent, and reasonable behavior with very few exceptions. Furthermore, the data were in good agreement with the experimental data of Silhan and Cubbage,² which was independently considered by other investigators to contain very

reliable data.²⁵ Values of boattail drag coefficients from other sources generally tended to be higher than those from References 1 and 2 and introduced only a scatter of the data points. The experiments reported in References 1 and 2 were performed at Mach numbers from 0.6 to 1.28 (1.3), and with conical afterbodies having boattail angles $\beta = 3.0, 5.6, 8.0, 16.0, 30.0$, and 45.0 deg. The diameter ratio d_b/d_m of the experimental models was 0, 0.55, 0.7, and 0.85. The afterbodies of Reference 1 had annular base areas with $d_j/d_b = 0.65$ and 0.75 . Data taken from Reference 2 were for open base areas.

Figure 3 shows the boattail pressure drag coefficient $C_{D\beta}$ as a function of β and $(d_b/d_m)^2$. The particular form of presentation was chosen because of ease of interpolation during use of the graphs. The graphs were obtained by cross plotting for each Mach number graphs of the type shown in Figure 4. The data points in Figure 4 were obtained from Reference 1 (jet-off case) and from Reference 2, which had a model with a solid flat base and no nozzle provisions. Only values of β up to 16 deg were used.

There is a noticeable change in the character of the constant β curves in Figure 3 as well as the $C_{D\beta}$ values themselves between Mach numbers 0.6 and 0.9. The trend continues in the supersonic range, although after $M = 1.1$, the relative values of the $C_{D\beta}$ are decreasing as would be expected. The change of $C_{D\beta}$ values between Mach numbers 0.6 and 0.9 is particularly significant for the lower $(d_b/d_m)^2$ ratios and $\beta > 8$ deg. Note that in the supersonic case, the $C_{D\beta}$ values continue to increase as the $(d_b/d_m)^2$ ratio approaches zero. This is in contrast with the circular arc afterbodies, in which case the boattail pressure coefficient $C_{D\beta}$ reaches maximum values somewhere between $0 < (d_b/d_m)^2 < 1.0$.

Base Drag

Figure 5 presents the base pressure coefficient C_{pb} as a function of β and $(d_b/d_m)^2$ at the same Mach numbers from 0.6 to 1.3. Data in Figure 5 were taken from References 1 and 3. There was generally a systematic, consistent, and reasonable agreement between the data from the two references with a small number of exceptions. Data from Reference 3 were taken for the open base configuration. The average difference in base drag

coefficient between an open base and a flat base conical afterbody is about 0.01, according to the experiments of Reference 3, with the flat base giving a higher base drag coefficient. According to Cubbage and Andrews⁵ and Kurn,⁸ the variation of base pressure over the drag-producing base area in a radial direction is fairly insensitive for the jet-off case, although some variation usually does occur in the jet-on case. The base drag coefficients in Reference 1 were computed using pressure measurements at the base annulus only, while the same coefficients in Reference 3 were computed from pressure measurements at the open base.

The graphs in Figure 5 were obtained by the following method. When the base pressure coefficient C_{pb} was plotted against $(d_b/d_m)^2$ for constant values of β , it was noted that the resulting behavior of the constant β points was very regular and consistent at all Mach numbers. In fact, whenever three points for the β were available at different $(d_b/d_m)^2$ ratios, the trend of the C_{pb} curves as a function of $(d_b/d_m)^2$ was generally linear. Consequently, it was assumed that for $(d_b/d_m)^2 > 0.1$, C_{pb} is essentially a linear function of $(d_b/d_m)^2$. In the vicinity of $(d_b/d_m)^2 = 1.0$ it was assumed that the C_{pb} converges to the value of C_{pb} for a cylindrical afterbody. The basic pattern occurred consistently at all Mach numbers from 0.6 to 1.3 for data from References 1 and 3. Moreover, data from Reference 1 was for an annular base with $d_j/d_b \approx 1$. Data from Reference 2 and Reference 1 at $d_j/d_b = 0.65$ did not generally follow this consistent pattern and were not used for establishing the correlation; however, data from Reference 1 for $d_j/d_b = 0.65$ are shown in Figure 6 at some angles of β , e.g., $\beta = 5.6$ and 16 deg. Note that with respect to the boattail drag coefficient, the agreement between References 1 and 2 was generally very good, being consistent at all Mach numbers of the experiments.

The base pressure coefficients for a cylinder were chosen from the available published data at the respective Mach numbers to correlate with the experimental data used in the present investigation. These data and the C_{pb} values for a cylindrical afterbody used in the present correlation are shown in Figure 7. Because the mean value of the $(d_b/d_m)^2$ ratios used in the correlation was in the vicinity of 0.6, which also represents a significant point in practical applications, $(d_b/d_m)^2 = 0.6$ was chosen as a reference point in the graphs of the type shown in

Figure 6. The slope $\partial(C_{pb})/\partial(d_b/d_m)^2$ and the C_{pb} values from the dashed lines at $(d_b/d_m)^2 = 0.6$ were plotted versus β as shown in Figure 7, and the C_{pb} and the slope curves were fitted through the data points. The resulting slopes and C_{pb} values were superimposed on Figure 6 from which Figure 5 was obtained by cross-plotting C_{pb} as a function of β for constant $(d_b/d_m)^2$ values. The general character of the correlation shown in Figure 6 was typical for all Mach numbers.

DRAG OF CIRCULAR ARC AFTERBODIES

Boattail Drag

Experimental data for the correlation of circular arc boattail drag were taken from References 2, 8, 9, and 10. Reference 2 provides systematic experimental data for circular arc afterbodies as well as conical afterbodies. As mentioned, the conical afterbody experimental data of Reference 1 showed an exceptionally good agreement with the corresponding data from Reference 2. It would be reasonable to expect the same reliability with respect to the circular arc experimental data of Reference 2, particularly in view of the evaluation by others²⁵ of the reliability of the data contained in Reference 2. Moreover, there is also a reasonably good agreement of the circular arc boattail drag between Reference 2 and References 8, 9, and 10. In comparable cases, there was also quite good agreement with the data from unpublished DTNSRDC experiments. Experiments reported in Reference 2 were performed at Mach numbers from 0.6 to 1.3 for solid flat base circular arc boattails with boattail angles $\beta = 0, 3, 5.6, 8, 16,$ and 45 deg and d_b/d_m ratios of 0, 0.55, 0.7, and 0.85. Experiments reported in Reference 10 had circular arc boattails with boattail angles of 15.8, 27.5, and 34 deg and substantially open base areas. In addition, test results of a circular arc reference nozzle with a boattail angle of 21.57 deg were also included. Experiments reported in Reference 9 had circular arc boattails with $\beta = 8.3, 11, 14.8, 16.5,$ and 22.1 deg. Experiments reported in Reference 8 were performed with a tangent ogive and progressively truncated versions of it with boattail angles of 4.4, 9.6, 14.6, and 17.1 deg.

Figure 8 shows the boattail pressure drag coefficient $C_{D\beta}$ as a function of β and $(d_b/d_m)^2$. The typical graph shown in Figure 9 was obtained by fairing curves through $C_{D\beta}$ values for constant d_b/d_m ratios using data from References 2, 8, 9, and 10. Figure 8 was then obtained by cross-plotting $C_{D\beta}$ values for constant boattail angles β from Figure 9. Thus, for each β curve in Figure 8, five points (at five d_b/d_m values) were available. Additional experimental data for d_b/d_m values other than 0, 0.55, 0.7, and 0.85 were used to check the correlation.

A major characteristic of Figure 9 is the steep drag rise at about 8-deg boattail angle. This steep drag rise for the $d_b/d_m = 0.85$ case, which is particularly distinctive for $M = 1.0$ and 1.1 shown in Figures 8(d) and 8(e), accounts for the characteristic increase of $C_{D\beta}$ at $\beta = 8$ deg and $d_b/d_m = 0.85$ shown in Figure 9. Because this characteristic occurred consistently at all Mach numbers from 0.8 to 1.3, it could not be regarded as an experimental error.

In comparing the $C_{D\beta}$ curves for circular arc afterbodies with the $C_{D\beta}$ curves for conical afterbodies, the main difference is in the character of the boattail pressure drag for $(d_b/d_m)^2$ ratios of less than about 0.3 to 0.5. While in the supersonic case, the $C_{D\beta}$ values for the conical boattails continue to rise at these d_b/d_m ratios, the corresponding $C_{D\beta}$ values for the circular arc boattails exhibit a clear tendency to decrease with decreasing d_b/d_m ratios.

For $(d_b/d_m)^2$ ratios approaching 1.0, the boundary of the maximum $C_{D\beta}$ values is approximately the same for both the conical and circular arc boattails at the higher Mach numbers investigated. With increasing boattail angles and decreasing d_b/d_m ratios, however, the circular arc boattail is definitely more advantageous.

Base Drag

Figure 10 presents the base pressure coefficient C_{pb} as a function of β and $(d_b/d_m)^2$ at Mach numbers from 0.6 to 1.3. Data in Figure 10 were taken from References 2, 8, 9, and 10. The experimental models of References 2 and 8 had solid flat bases. The models of References 9 and 10 had open bases with very small annular base areas.

The graphs in Figure 10 were obtained by a similar method used to obtain the base pres. res for the conical afterbody. However, some of the slopes of the base pressure coefficient C_{pb} as a function of boattail angle β could not be obtained directly for lack of suitable data. Consequently, some of the data points shown in Figure 12 do not represent actual experimental values but are extrapolations of available data. The data points and the correlation curves for a typical case are shown in Figure 11. As in the conical case, it was assumed that within the larger part of the $(d_b/d_m)^2$ range, the base pressure coefficient C_{pb} is essentially a linear function of $(d_b/d_m)^2$. This assumption appears to be justified on the basis of available data. The correlation shown in Figures 11 and 12 is typical for all investigated Mach numbers.

One notable difference between the graphs of Figure 10 for the circular arc afterbodies and the graphs of Figure 5 for the conical afterbodies is that the sensitivity of the base pressure coefficient C_{pb} with β in the lower β range is much more pronounced in the circular arc case. This may partly explain the increased scatter of experimental data for the circular arc afterbodies in the lower β range. The base pressure apparently may experience large variations with relatively small variations in model geometry.

Another characteristic of the base pressure coefficient for circular arc afterbodies is the apparent movement of the optimum boattail angle β from the vicinity of 24 deg at Mach number 0.6 to the vicinity of 16 deg for the supersonic case.

CIRCULAR ARC-CONICAL AFTERBODY COMBINATIONS

The effect of rounding off the corner at the cone-cylinder juncture of a basic conical boattail is generally beneficial, particularly if the round-off radius is larger than $2d_m$. This effect for a 15-deg conical boattail is reported in Reference 26.

In using Reference 26, it must be considered that the experiments have been performed and reported for sting-supported wind tunnel models. The effect of the sting may be evaluated from the information contained in Reference 7.

EFFECT OF REYNOLDS NUMBER

The results of this investigation have been presented under the assumption that the effect of Reynolds number may be ignored. This may be justified for preliminary design purposes in view of the present knowledge of this subject. The following discussion of the effect of Reynolds number pertains only to turbulent boundary layers within the subsonic and transonic Mach number range.

There appears to be some inconsistency in the published reports regarding the evaluation of the effects of Reynolds number on afterbody drag characteristics. Reference 27 presents data which show an extremely large dependency of boattail drag on Reynolds number. Conversely, Reference 28 shows that for practical purposes there is no effect of Reynolds number on the boattail drag of afterbodies. However, there exist significant differences between the conditions of the experiments reported in the two references. These differences may be reviewed in the light of the information and discussions contained in References 29 and 30. The results reported in Reference 27 were obtained from wind tunnel and flight tests. The afterbodies were tested as part of an aircraft configuration in a very complex flow field. Furthermore, most of the flight data were taken while in coordinated turns under an angle of attack and with load factors up to 2.5 g's.

Conversely, the results reported in Reference 28 were obtained only from wind tunnel experiments with sting-mounted, cone-cylinder-afterbody models. Models of similar configurations were also tested in the experiments reported in Reference 29. Although the three models tested in the experiment reported in Reference 29 showed some effect of Reynolds number, the effect on all the models was not consistent and, in any case, did not show the extreme drag variation with Reynolds number reported in Reference 27. Perhaps the most important conclusion of the report is that the absolute level of afterbody pressure drag can vary due to experimental factors such as tunnel characteristics and model installation. The same conclusion can be applied to flight tests. Also, changing the Reynolds number may alter the tunnel characteristics and, therefore, it may become difficult to isolate the two effects.

Reference 30 shows that the forebody configuration strongly influences the drag characteristics of the afterbody and vice versa. The report also concludes that the same afterbody tested as an isolated halfbody either in different wind tunnels or in the same tunnel with a different blockage will give very different afterbody drag values.

Conclusions based on the totality of the four reports are:

1. The effect, if any, of Reynolds number on afterbody drag for preliminary design purposes cannot be determined with any reliability.
2. The effect of Reynolds number on a specific configuration which includes afterbody must be determined for that particular configuration as a whole and not as a sum of the effects on the separate parts of the configuration.

SUMMARY

For smaller boattail angles β the boattail drag coefficient is relatively invariant with Mach numbers up to 0.9. At $M = 1$, an increase of the value of $C_{D\beta}$ plots show a marked regularity for Mach numbers below 0.9 and above 1.0, while the plots for $M = 0.9$ and 1.0 reflect the changes occurring in the flow regime in this transonic range.

At subsonic speeds, $C_{D\beta}$ is decreasing with decreasing $(d_b/d_m)^2$ ratio from a maximum at about $(d_b/d_m)^2 = 0.5$, suggesting a pressure recovery on the boattail. However, at supersonic speeds, such pressure recovery apparently does not occur.

The effect of boattailing on the base pressure is very apparent. At $M = 0.6$, C_{pb} is continuously increasing with increasing β and with decreasing $(d_b/d_m)^2$. However, already at $M = 0.8$, a marked change in the behavior of the base pressure starts to occur at β above approximately 10 deg. This behavior of the base pressure coefficient continues throughout the investigated range of Mach numbers above 0.6. Also, the effect of the $(d_b/d_m)^2$ in this transonic range becomes very noticeable, particularly at $M = 1.0$ and 1.1. The large positive base pressure coefficient is quite pronounced for boattail angles of around 12 deg. However, above $M = 1.0$, the area of positive pressure coefficient is shrinking quite noticeably with increasing Mach number.

The correlation in this investigation has been obtained assuming a turbulent boundary layer and a negligible effect of Reynolds number. This assumption appears to be justified in view of recent experiments.¹⁵

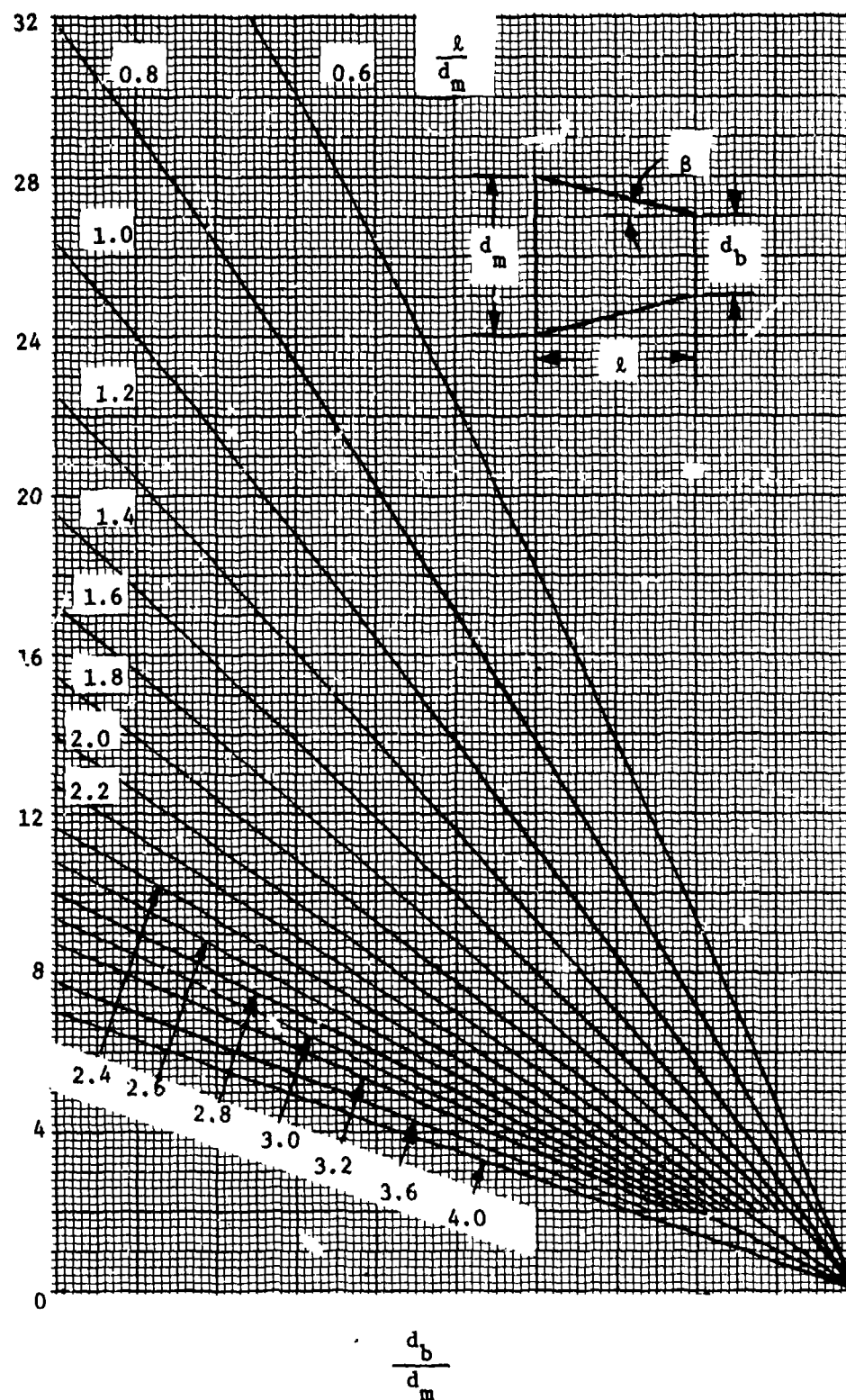


Figure 1 - Dimensionless Geometric Characteristics of Conical Boattails

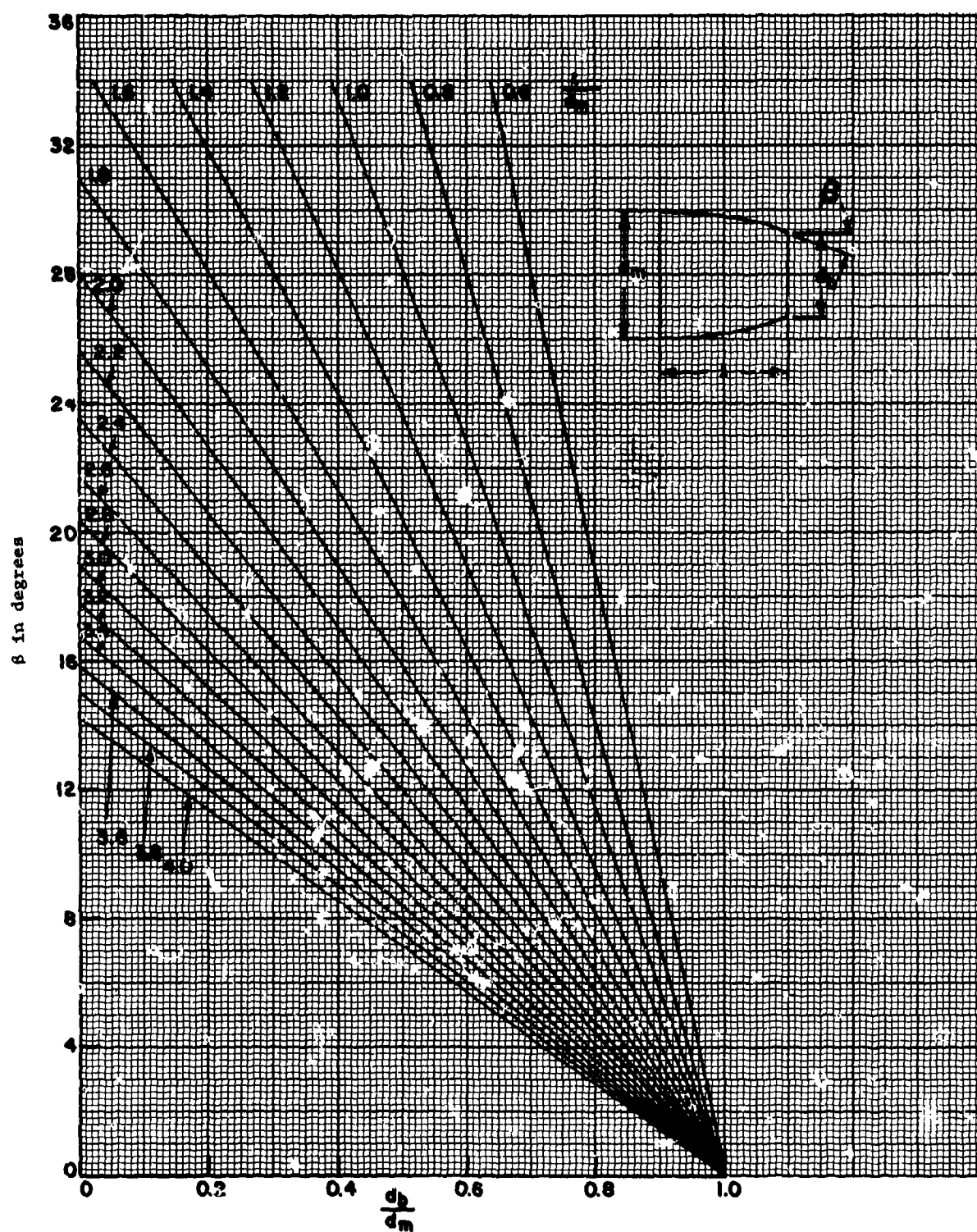


Figure 2 - Dimensionless Geometric Characteristics of
Tangent Circular Arc Boattails

Figure 3 - Conical Boattail Drag Coefficient with Jet Off

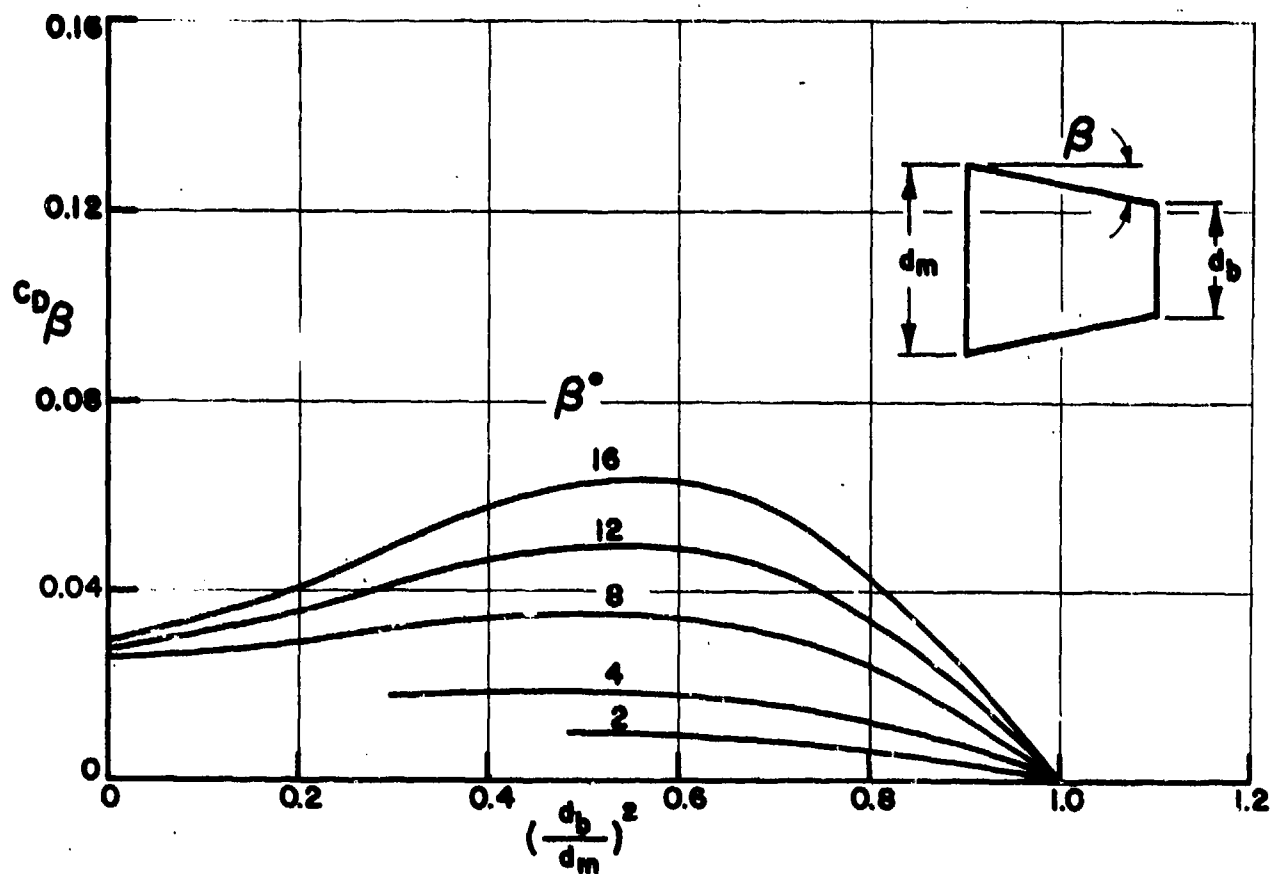


Figure 3a - $M = 0.6$

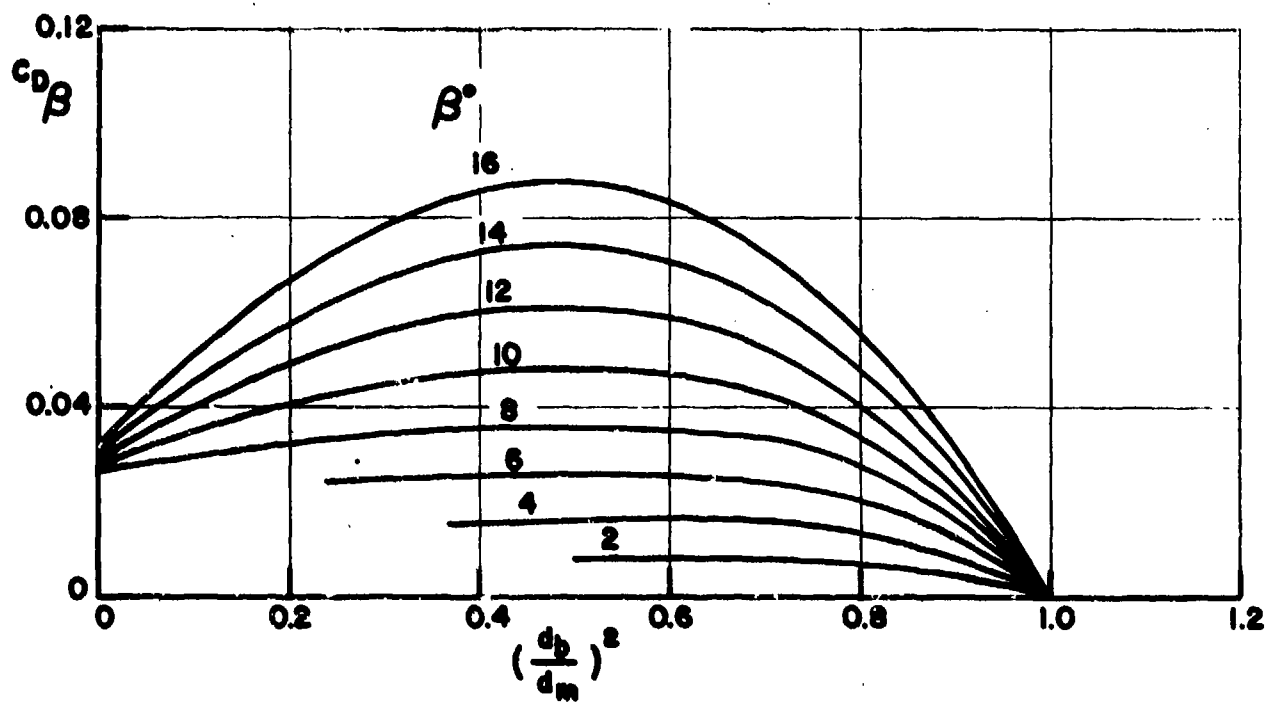


Figure 3b - $M = 0.8$

Figure 3 - Continued

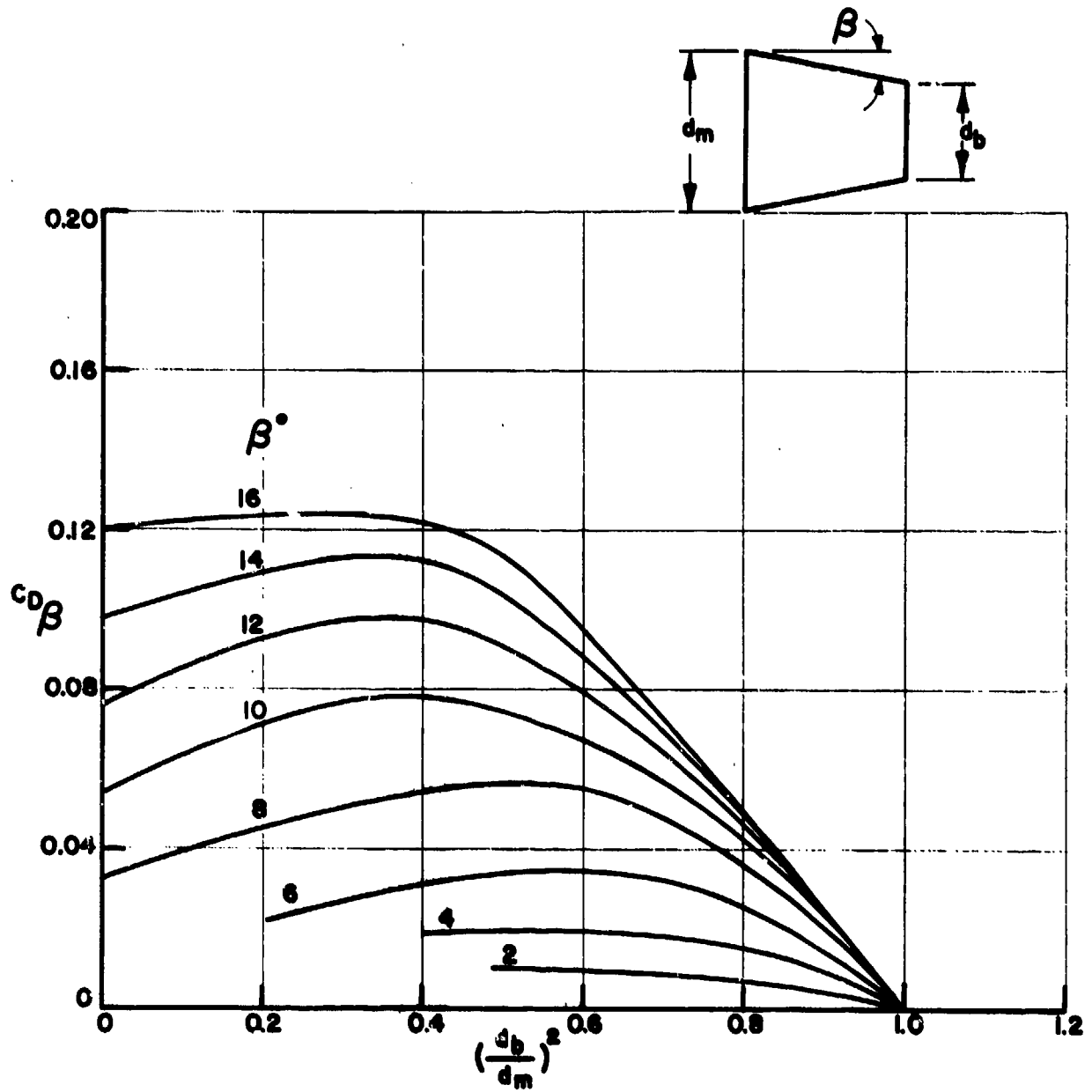


Figure 3c - $M = 0.9$

Figure 3 - Continued

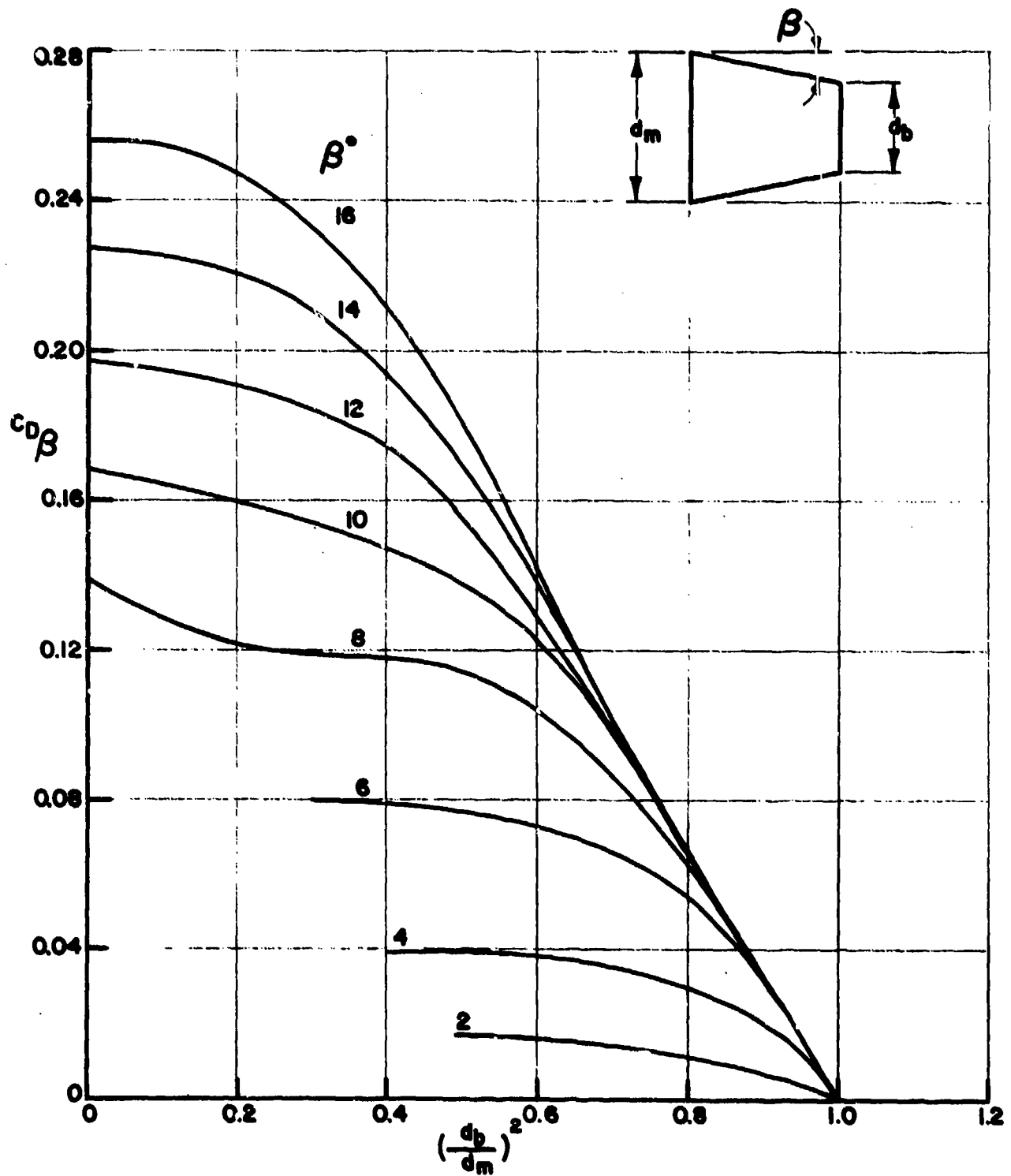


Figure 3d - $M = 1.0$

Figure 3 - Continued

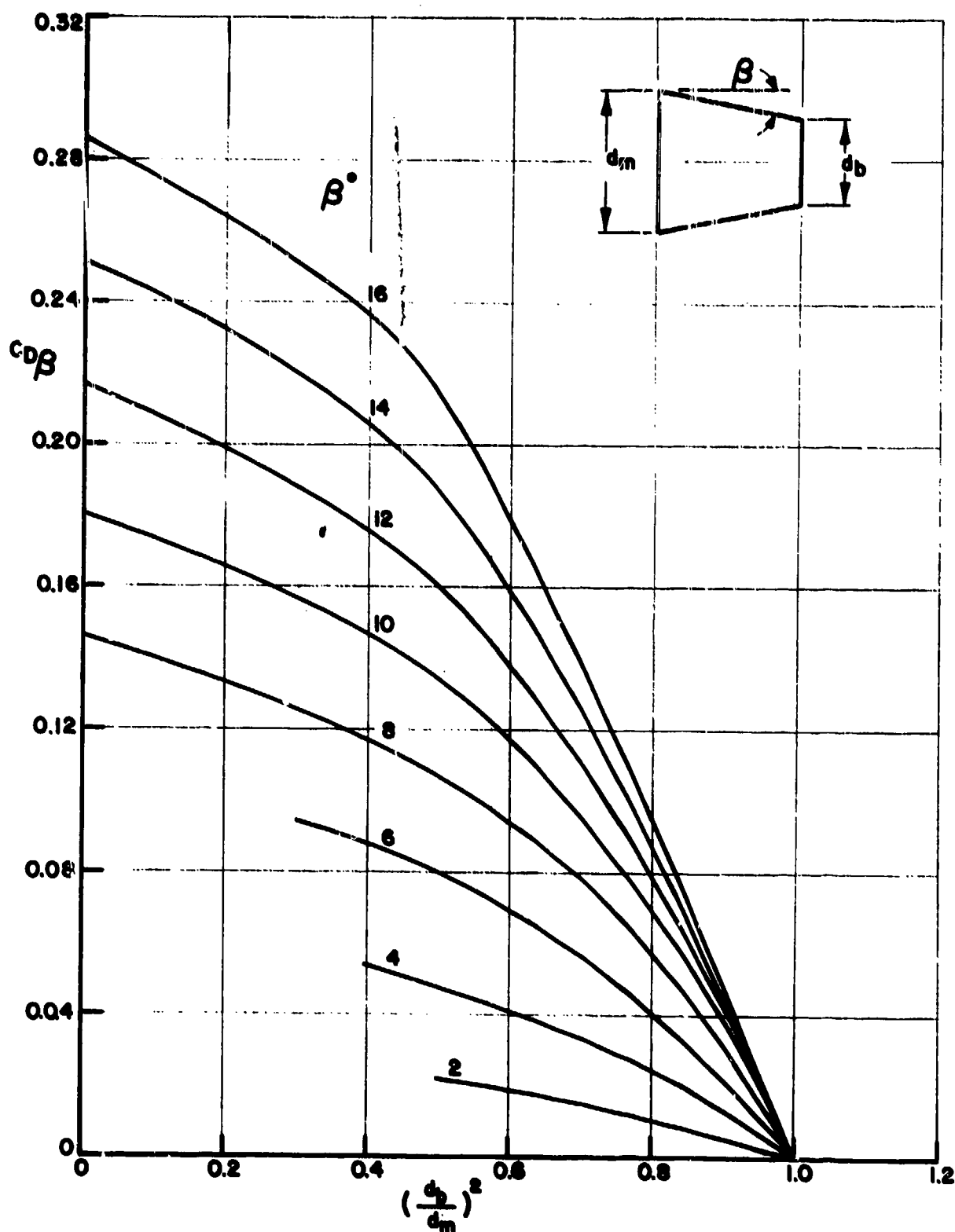


Figure 3e - $M = 1.1$

Figure 3 - Continued

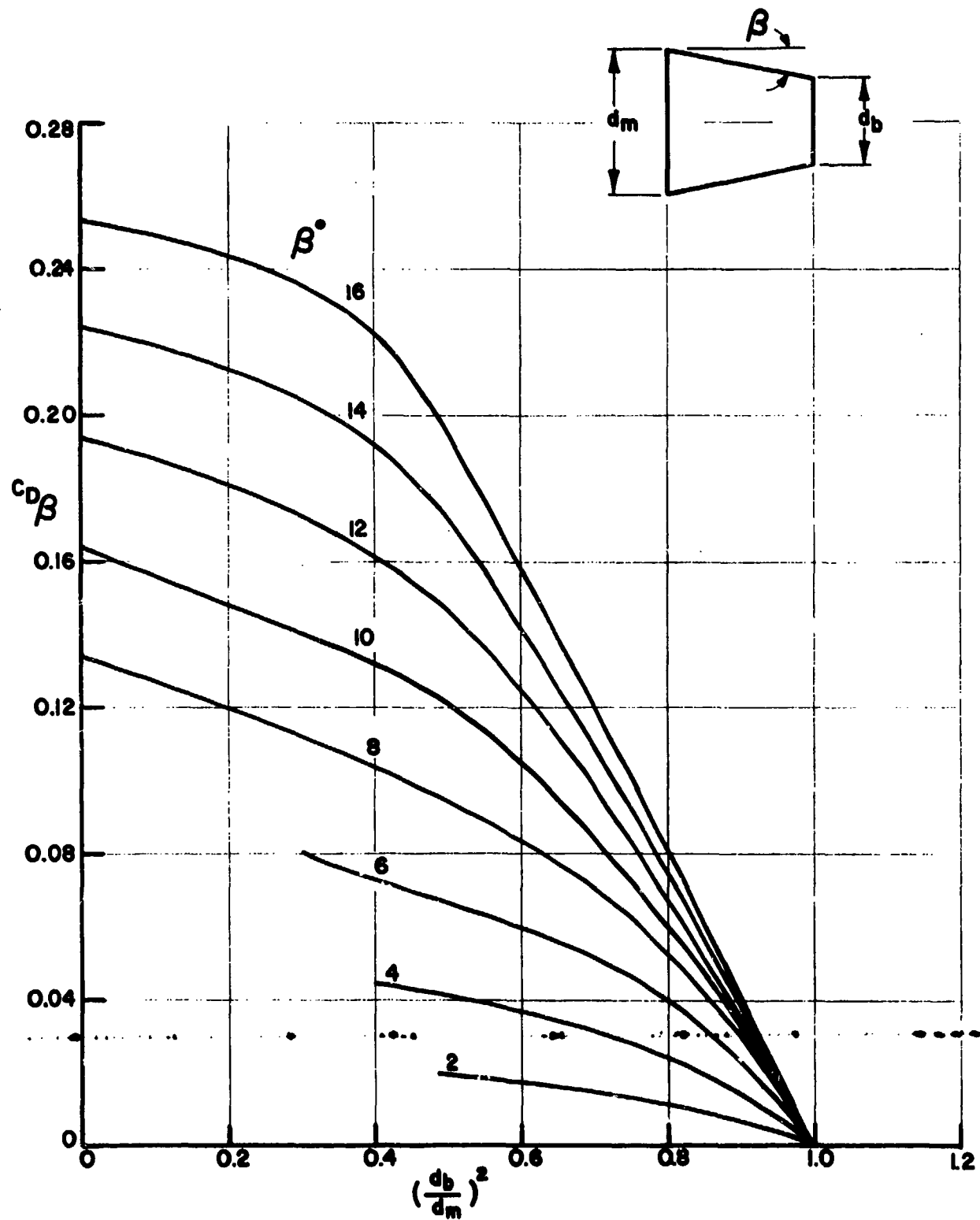


Figure 3f - M = 1.2

Figure 3 - Continued

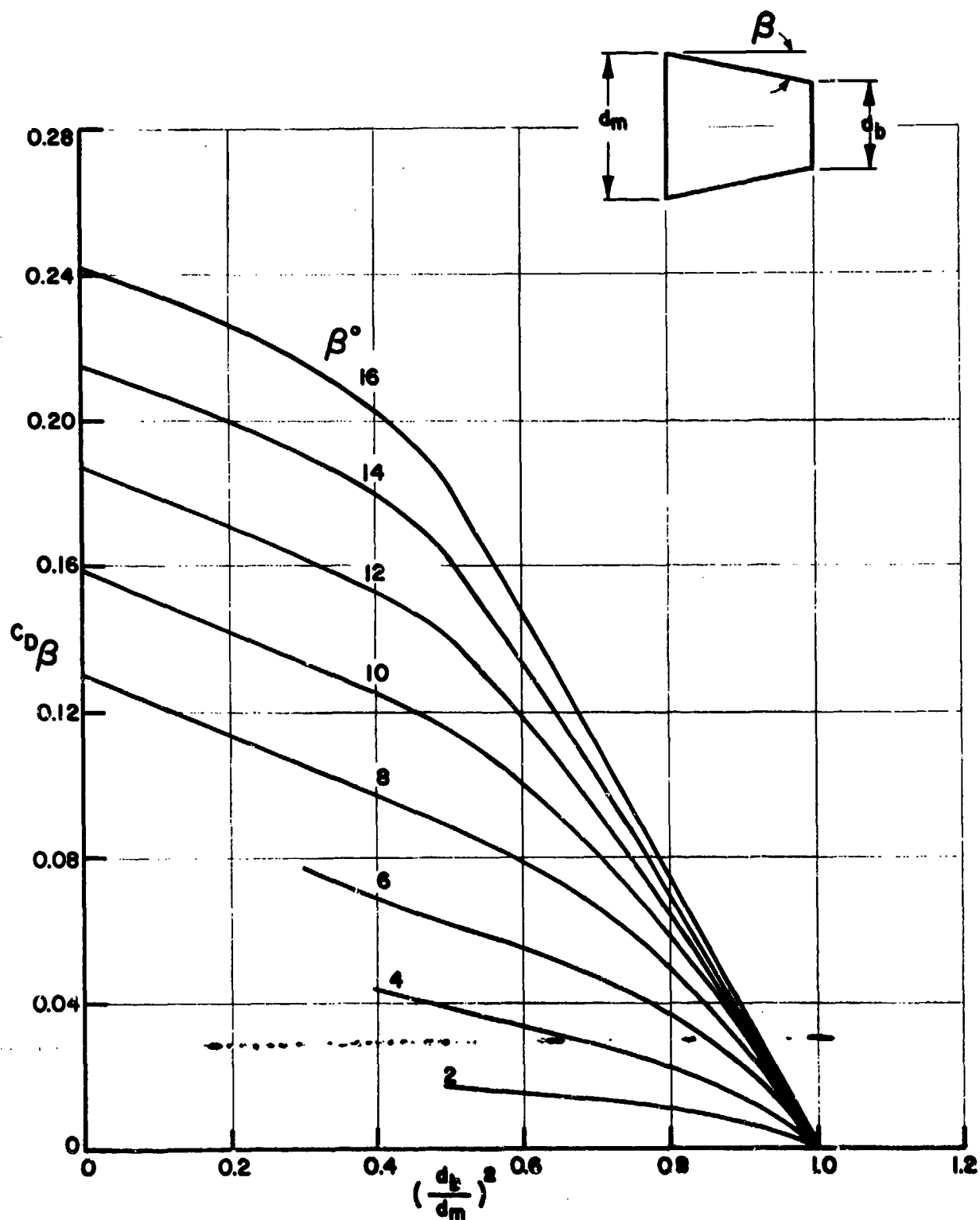


Figure 3g - $M = 1.3$

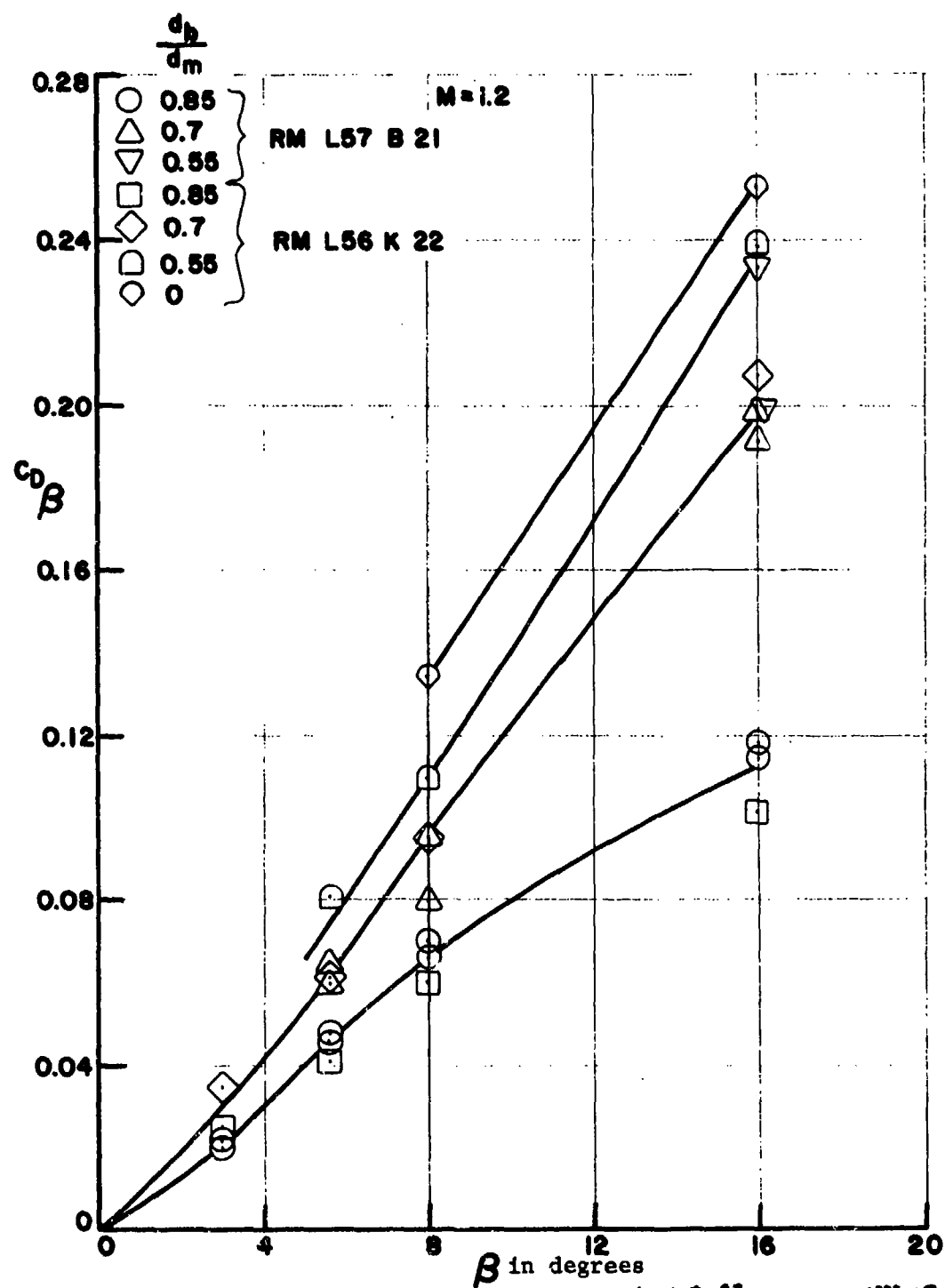


Figure 4 - A Correlation of Conical Boattail Drag Coefficients with Jet Off

Figure 5 - Conical Boattail Base Pressure Coefficients
with Jet Off

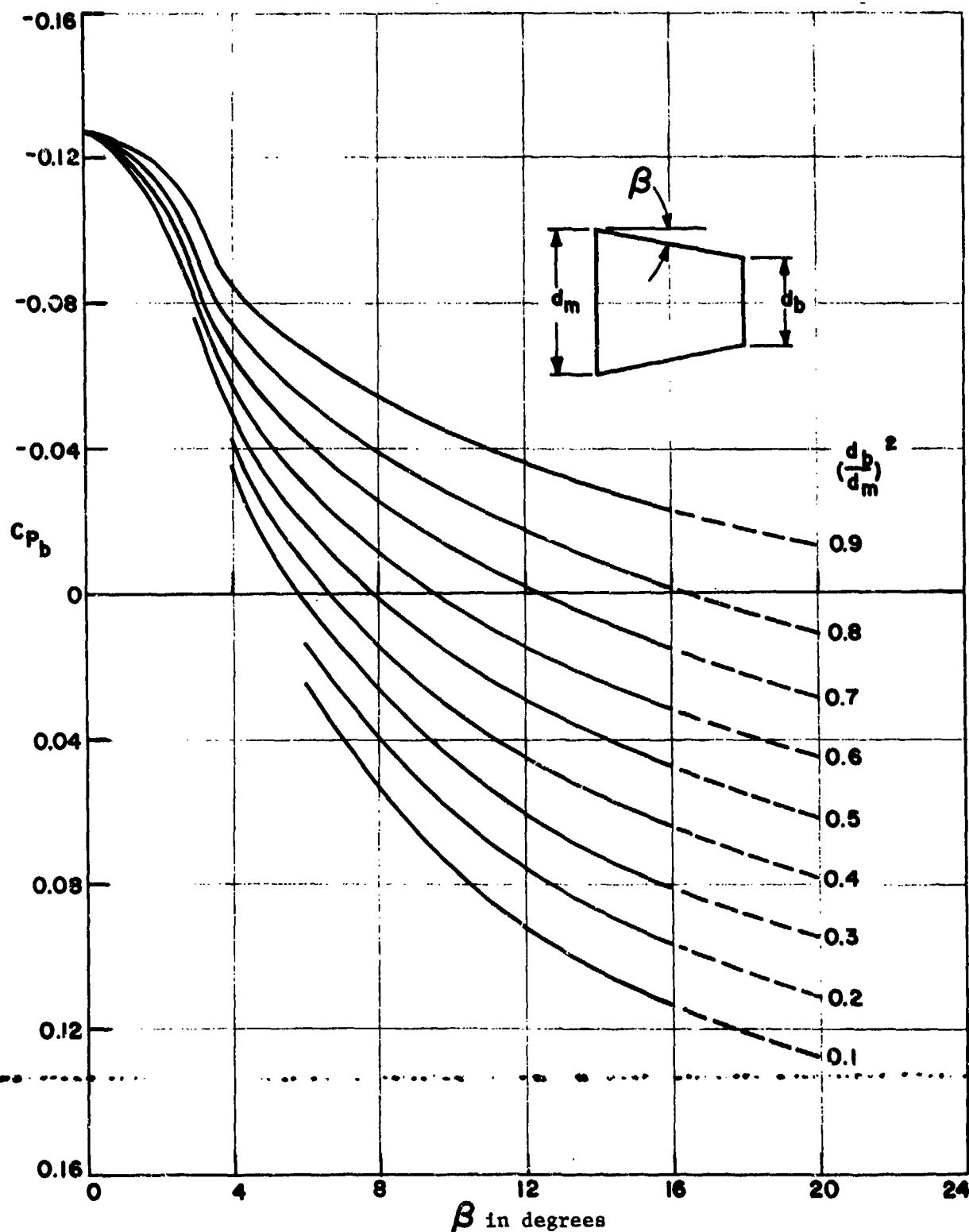


Figure 5a - $M = 0.6$

Figure 5 - Continued

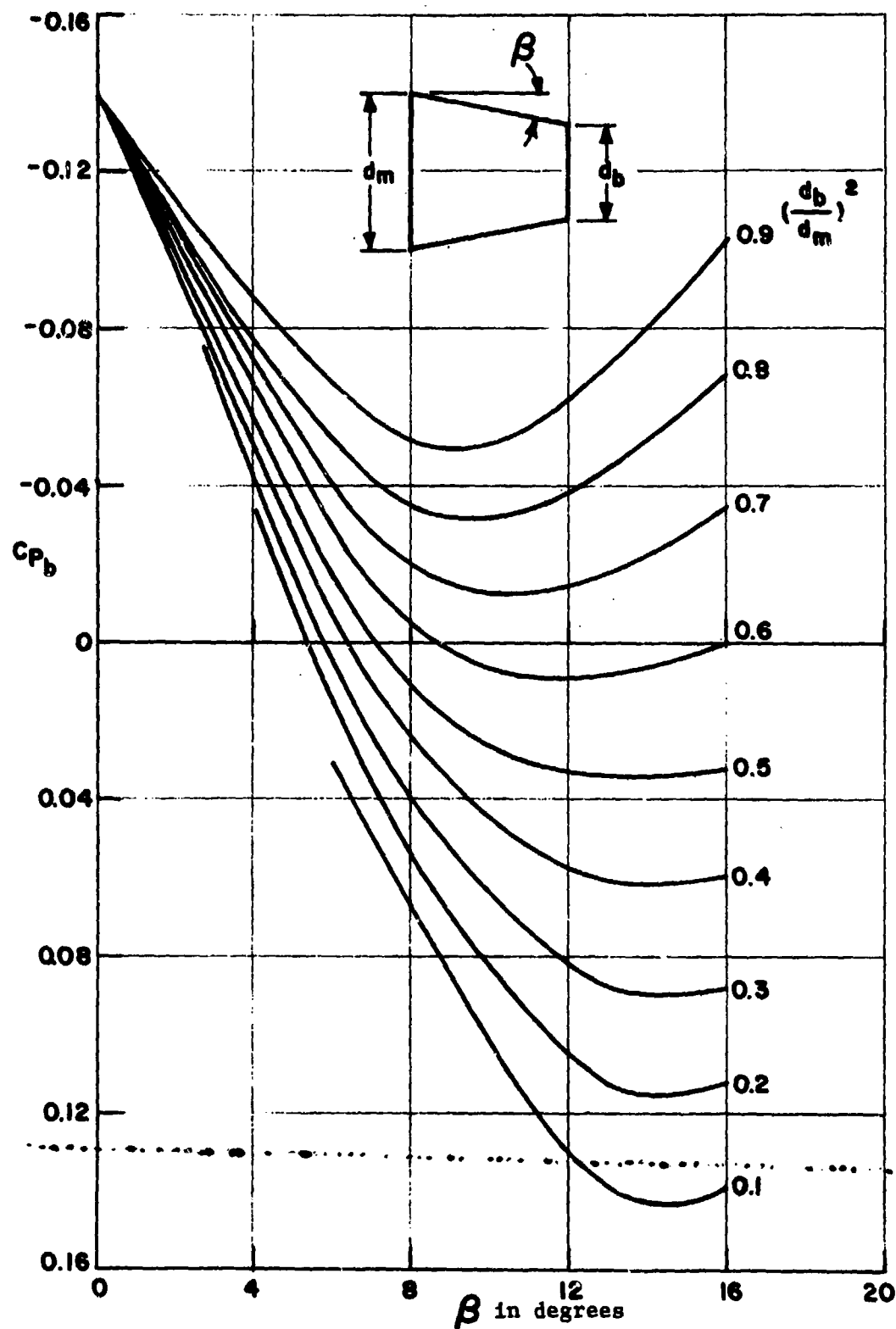


Figure 5b - M = 0.8

Figure 5 - Continued

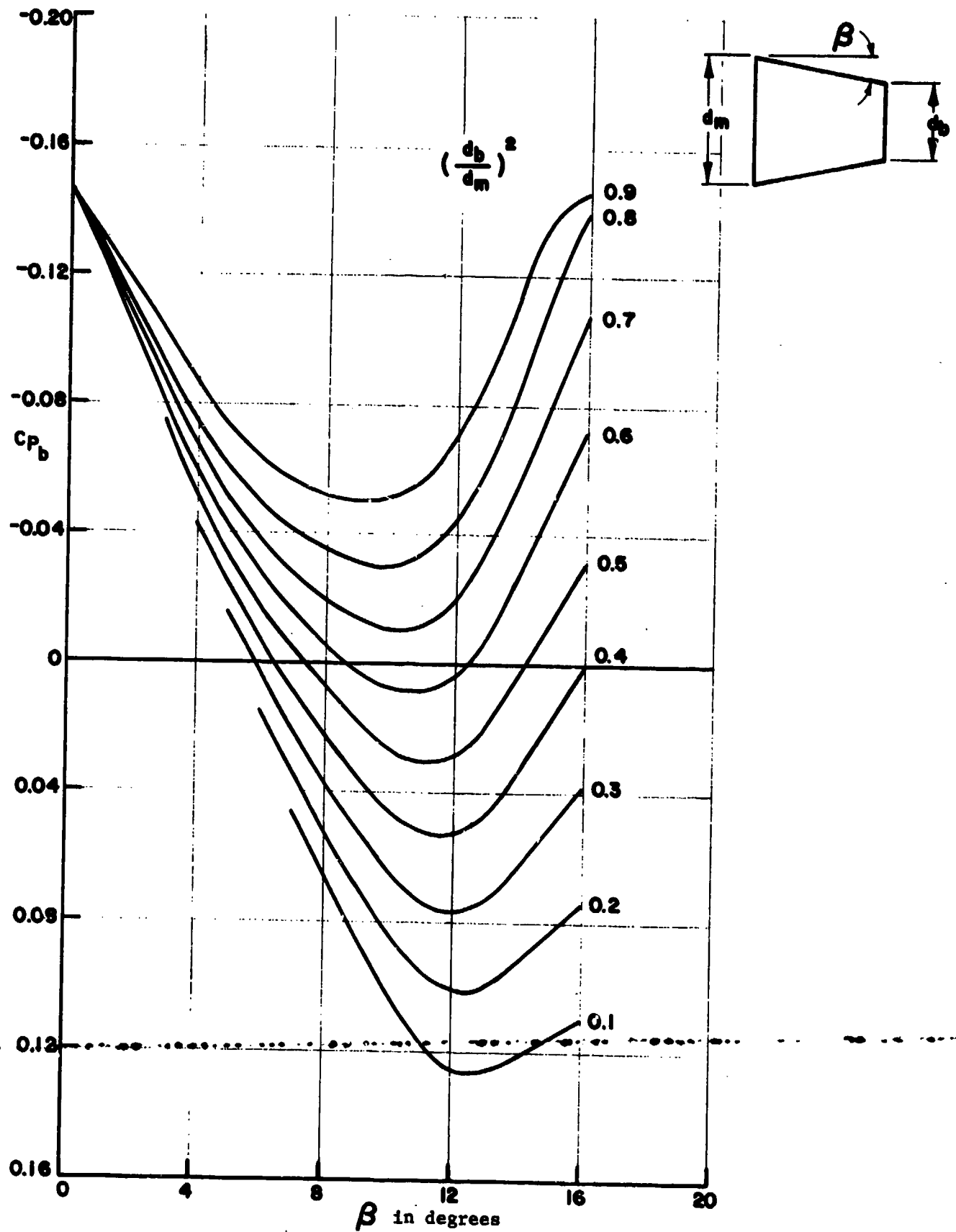
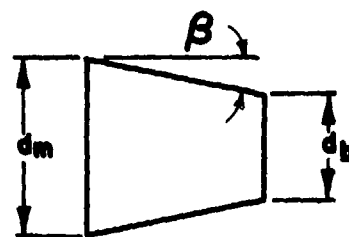
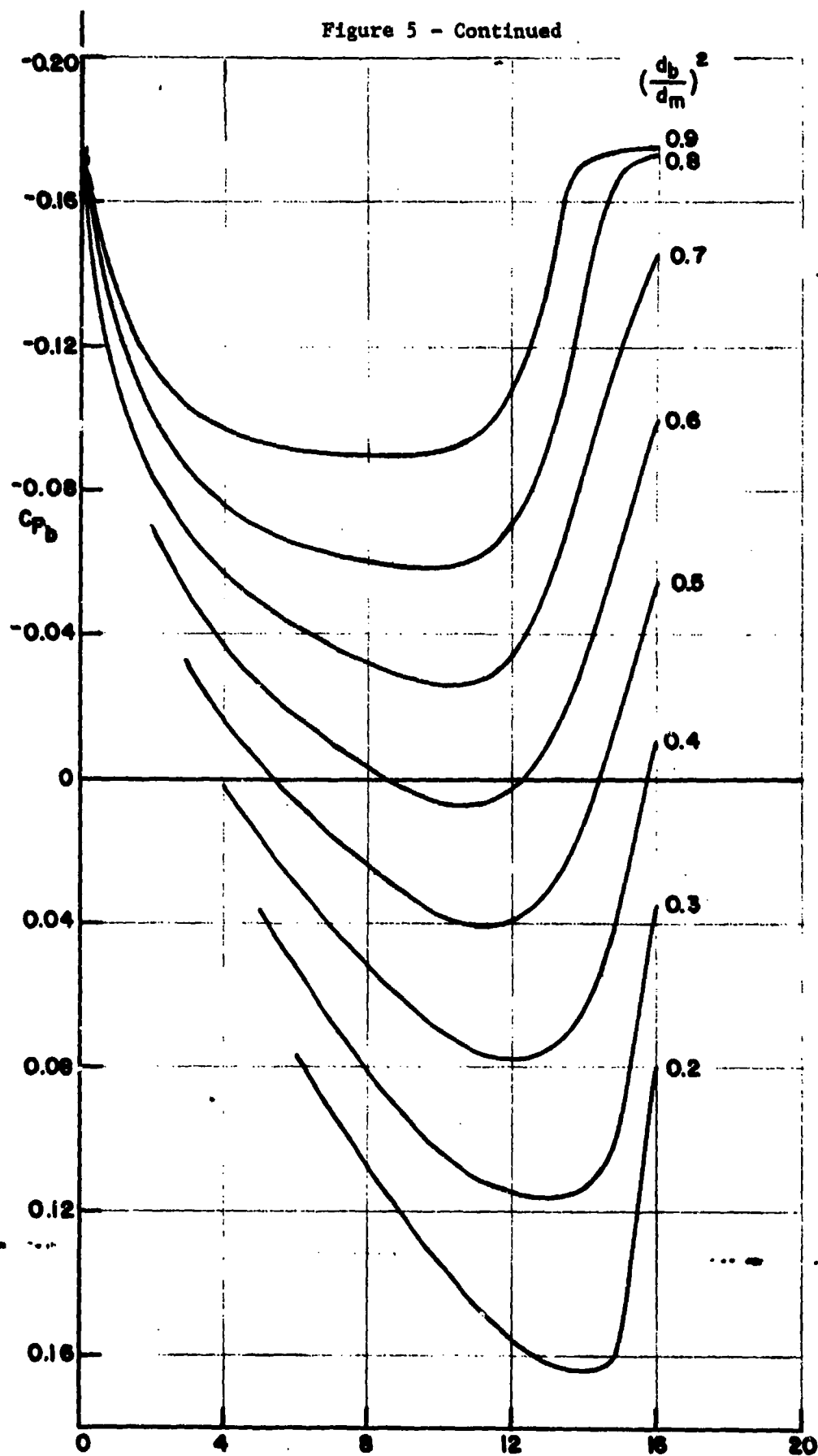


Figure 5c - $M = 0.9$

Figure 5 - Continued



β in degrees
Figure 5d - $M = 1.0$

Figure 5 - Continued

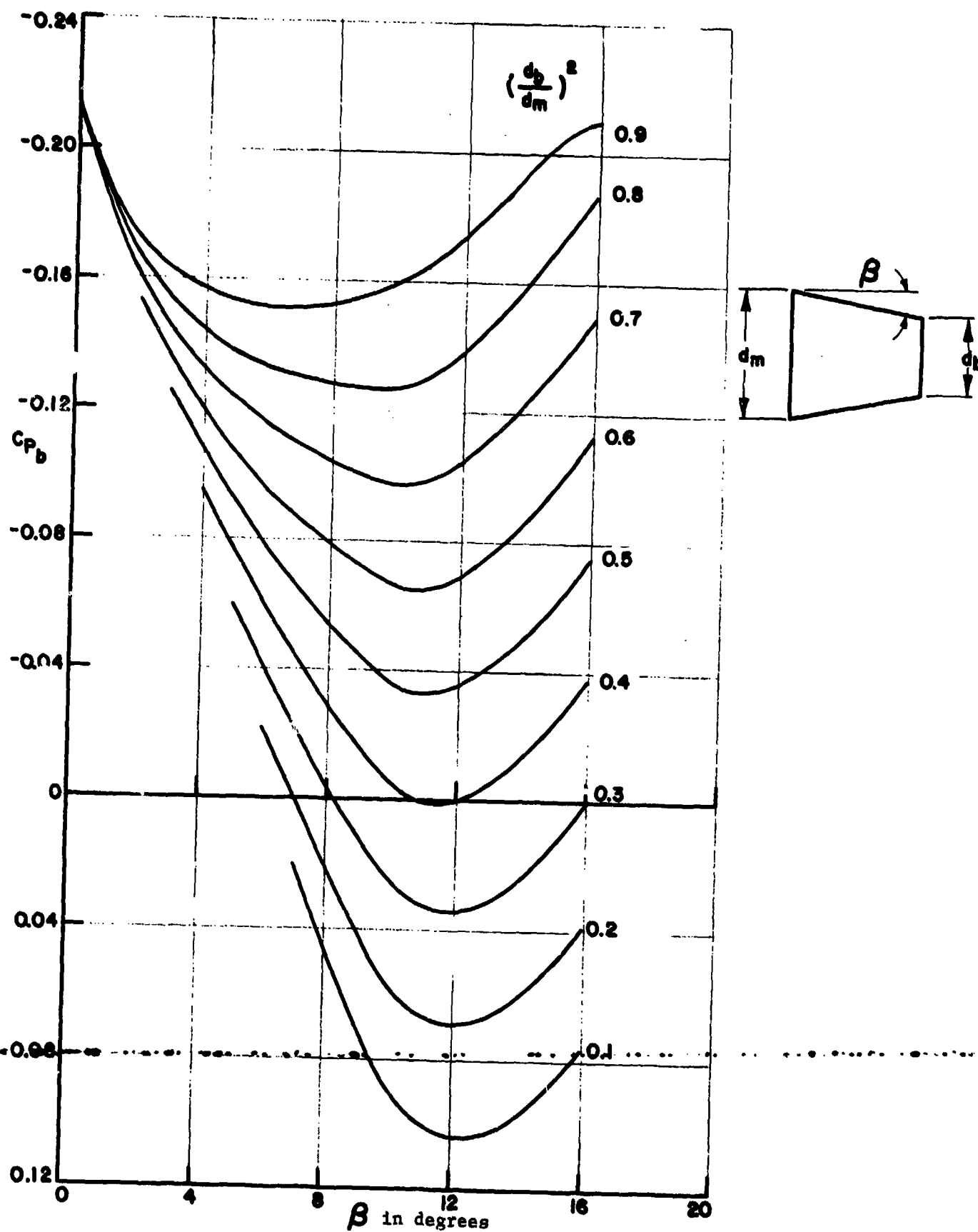


Figure 5e - $M = 1.1$

Figure 5 - Continued

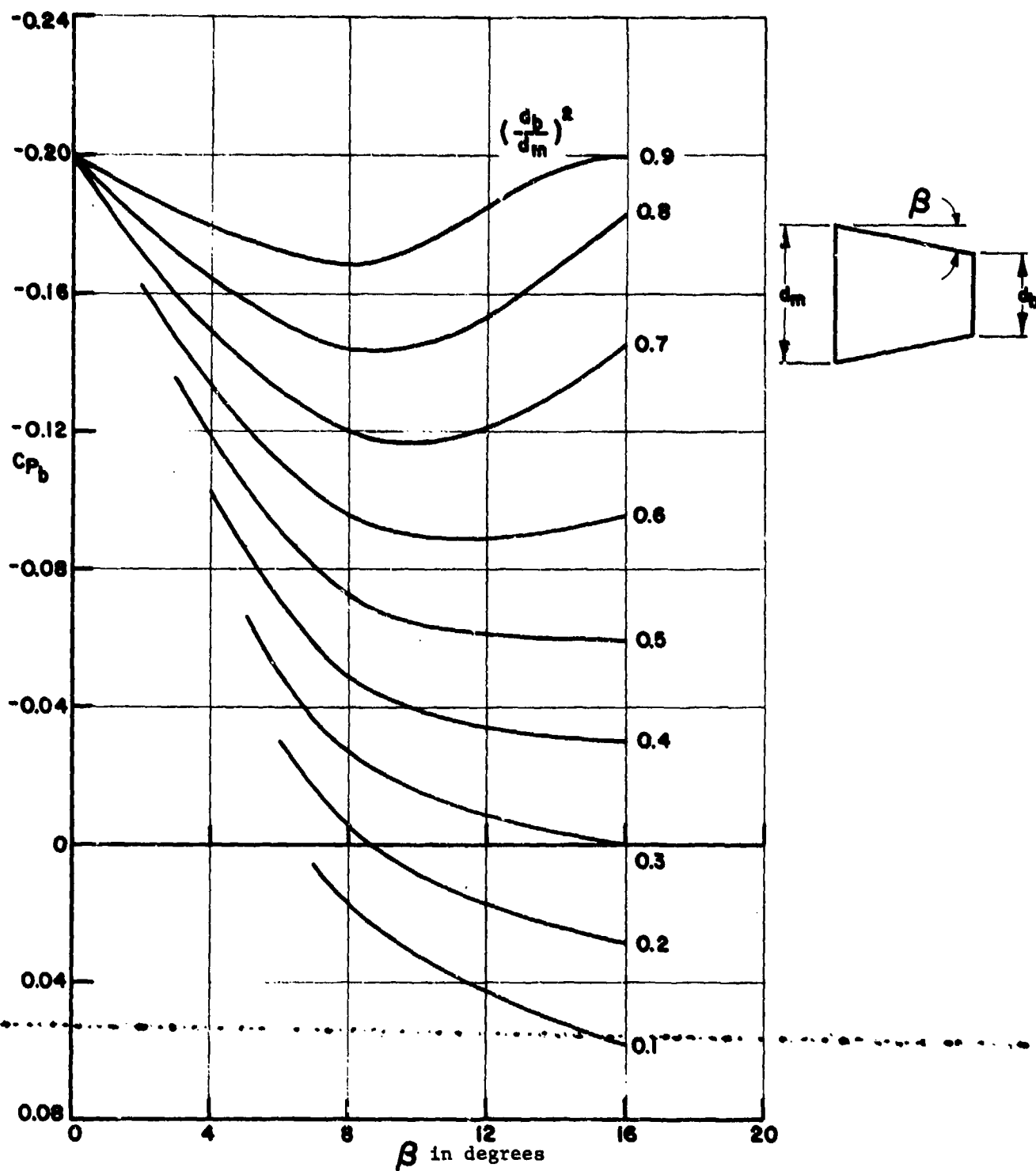


Figure 5f - $M = 1.2$

Figure 5 - Continued

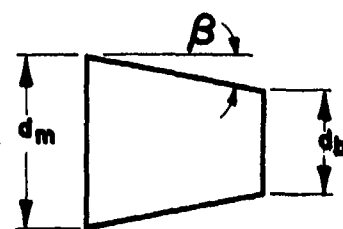
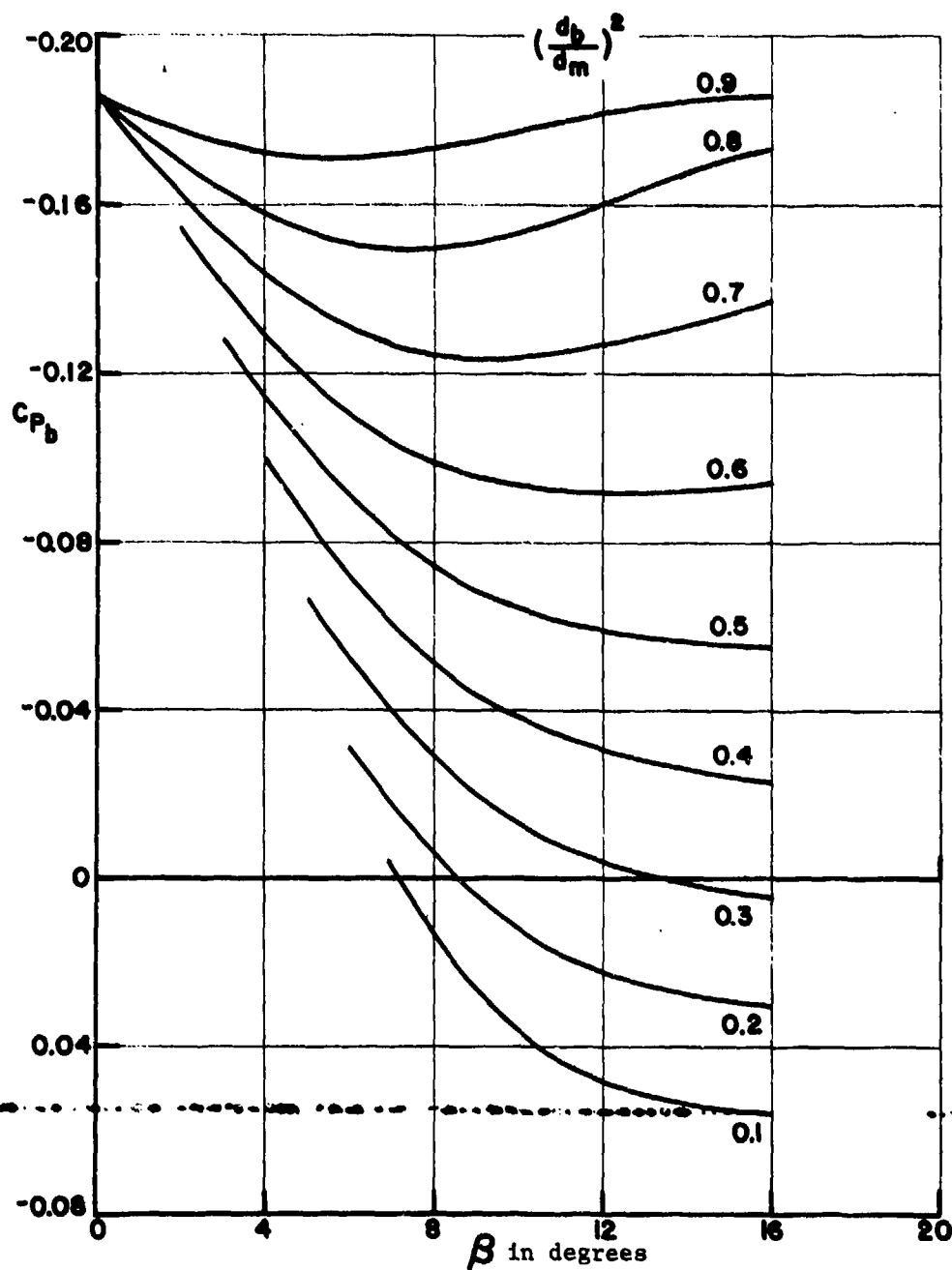


Figure 5g - $M = 1.3$

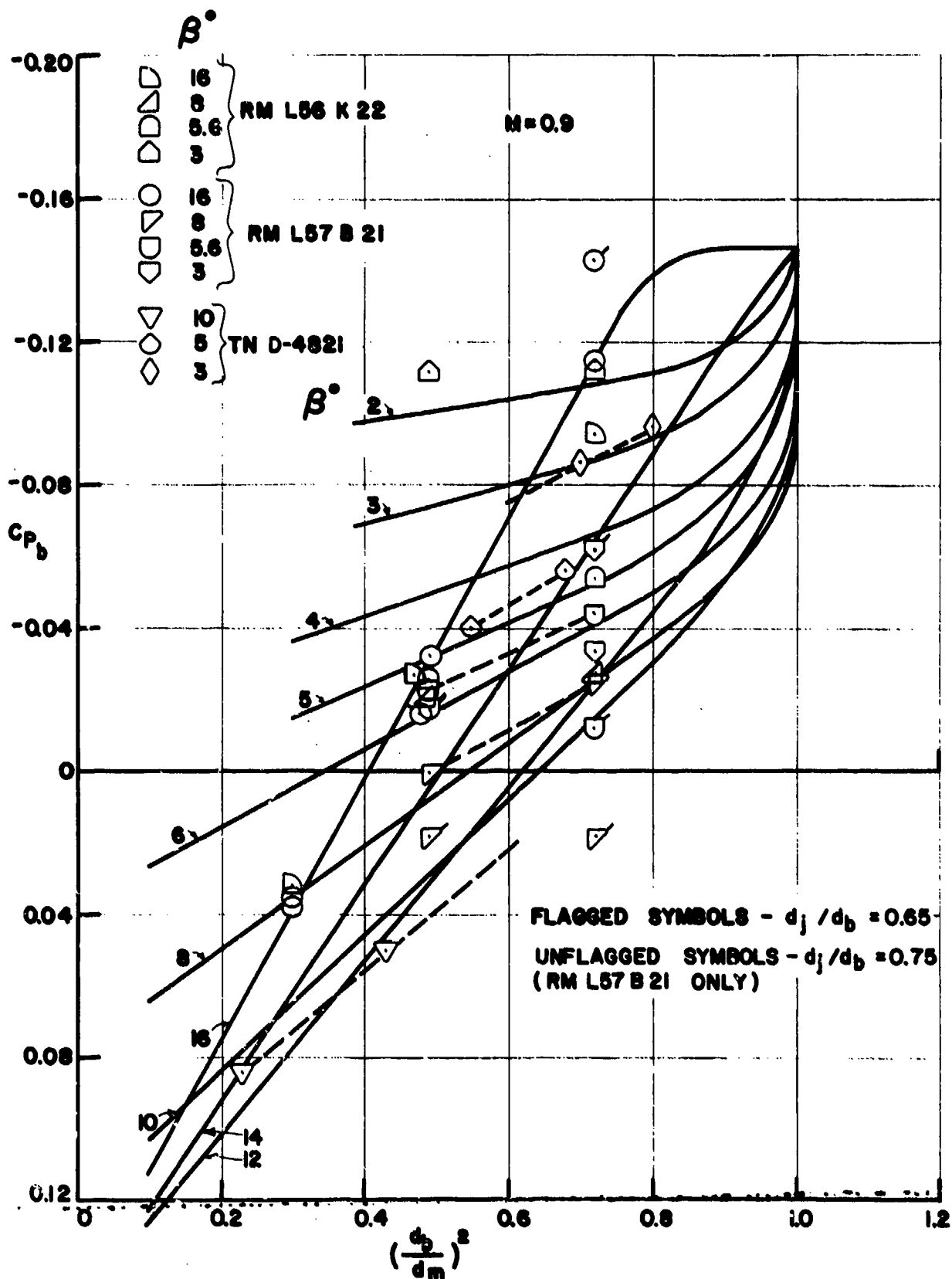


Figure 6 - A Correlation of Conical Boattail Base Pressure Coefficients as a Function of Base Diameter Ratio with Jet Off

RM L57 B 21
and
TN D-4821

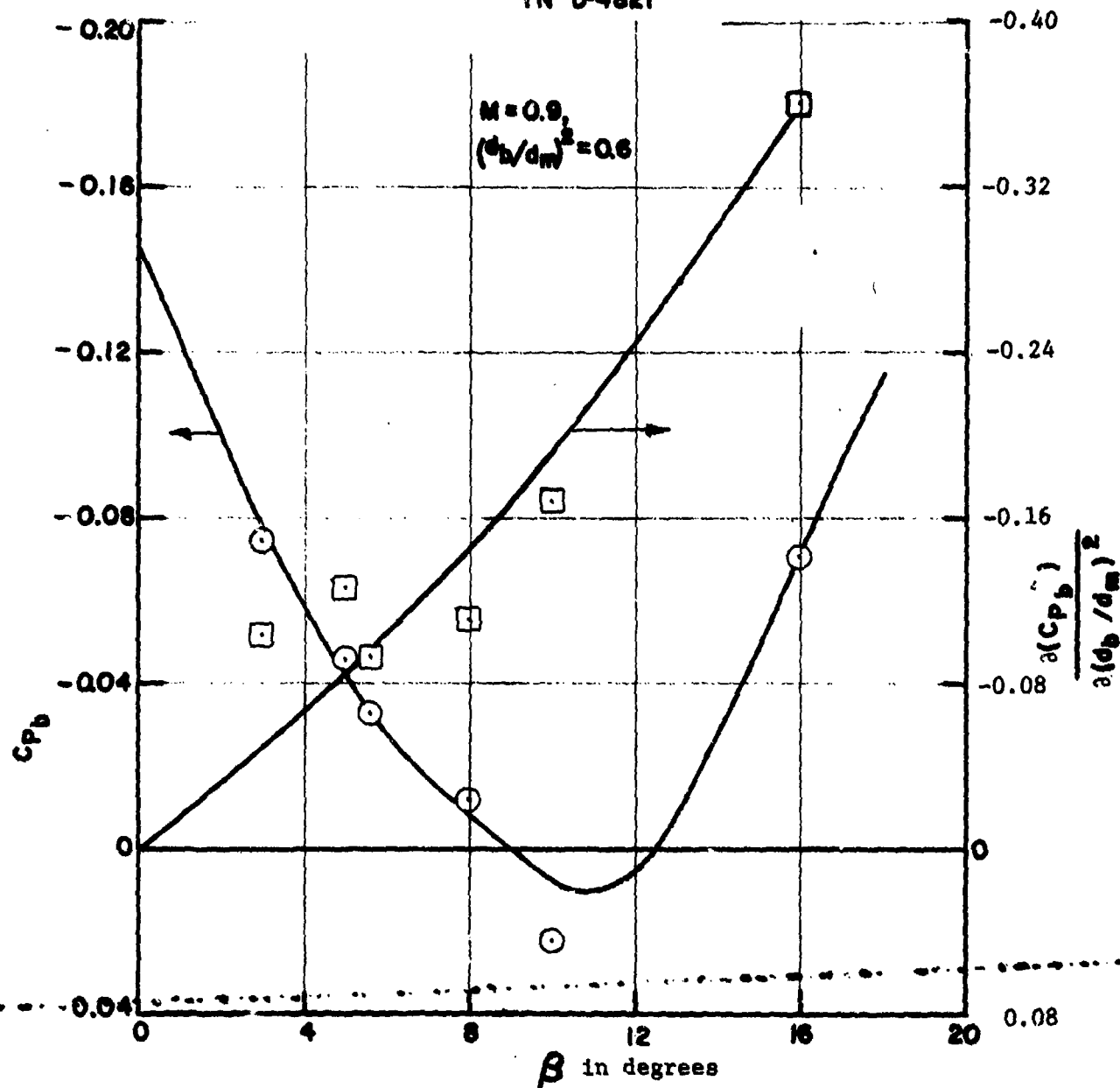


Figure 7 - A Correlation of Conical Boattail Base Pressure Coefficients as a Function of Boattail Angle with Jet Off

Figure 8 - Circular Arc Boattail Drag Coefficient with Jet Off

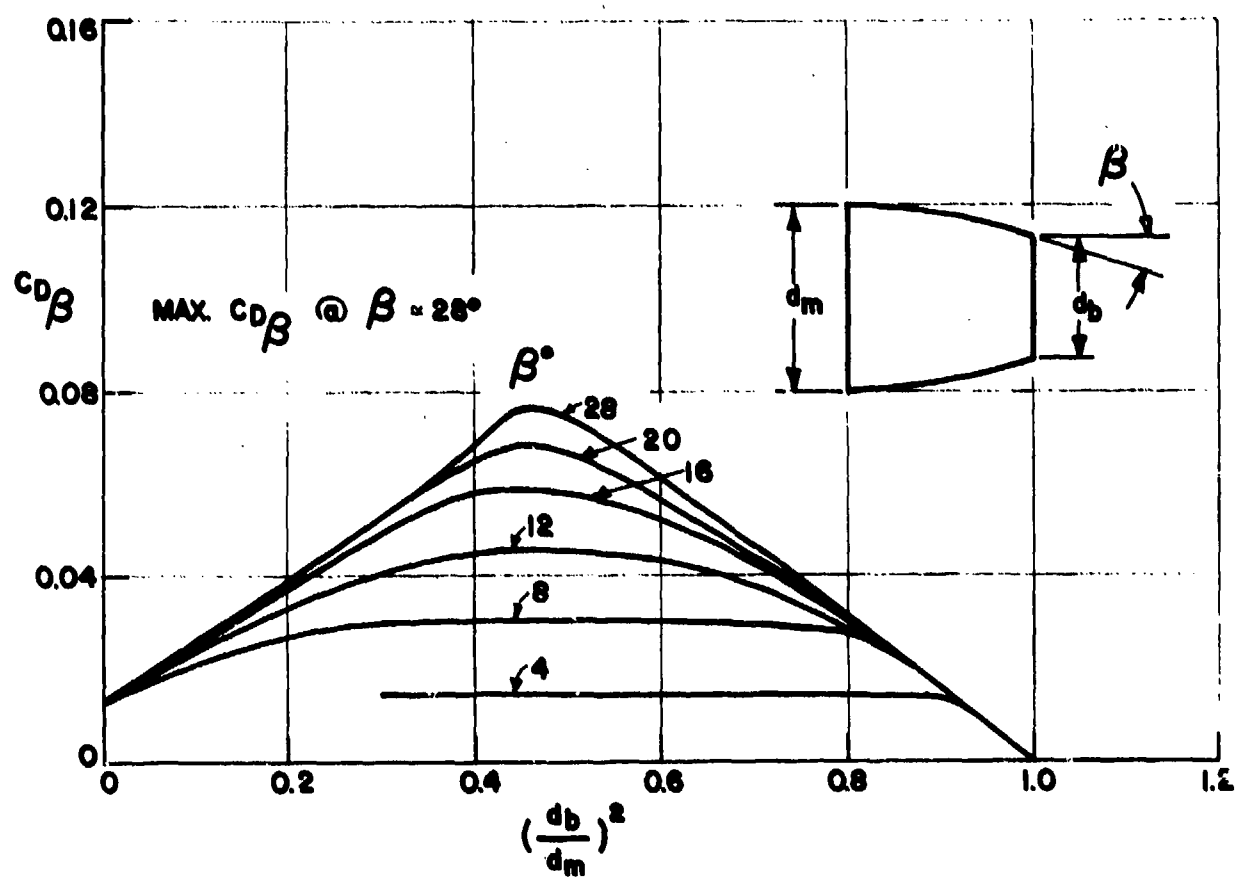


Figure 8a - $M = 0.5$

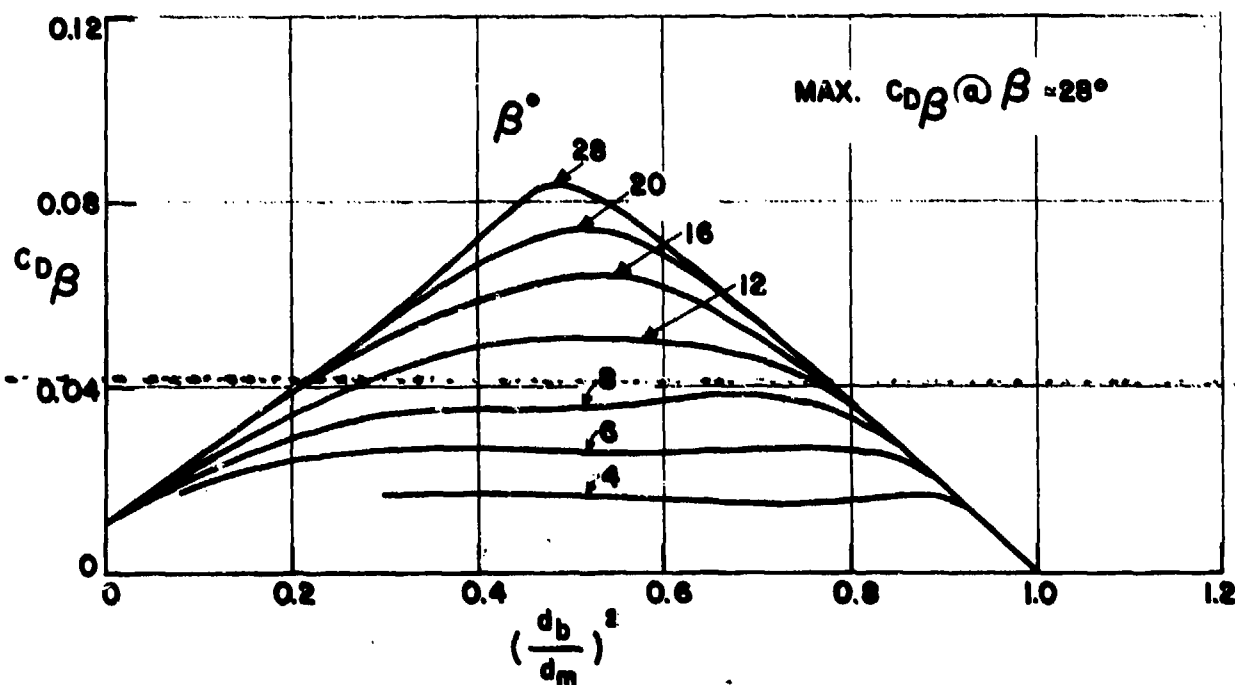


Figure 8b - $M = 0.8$

Figure 8 - Continued

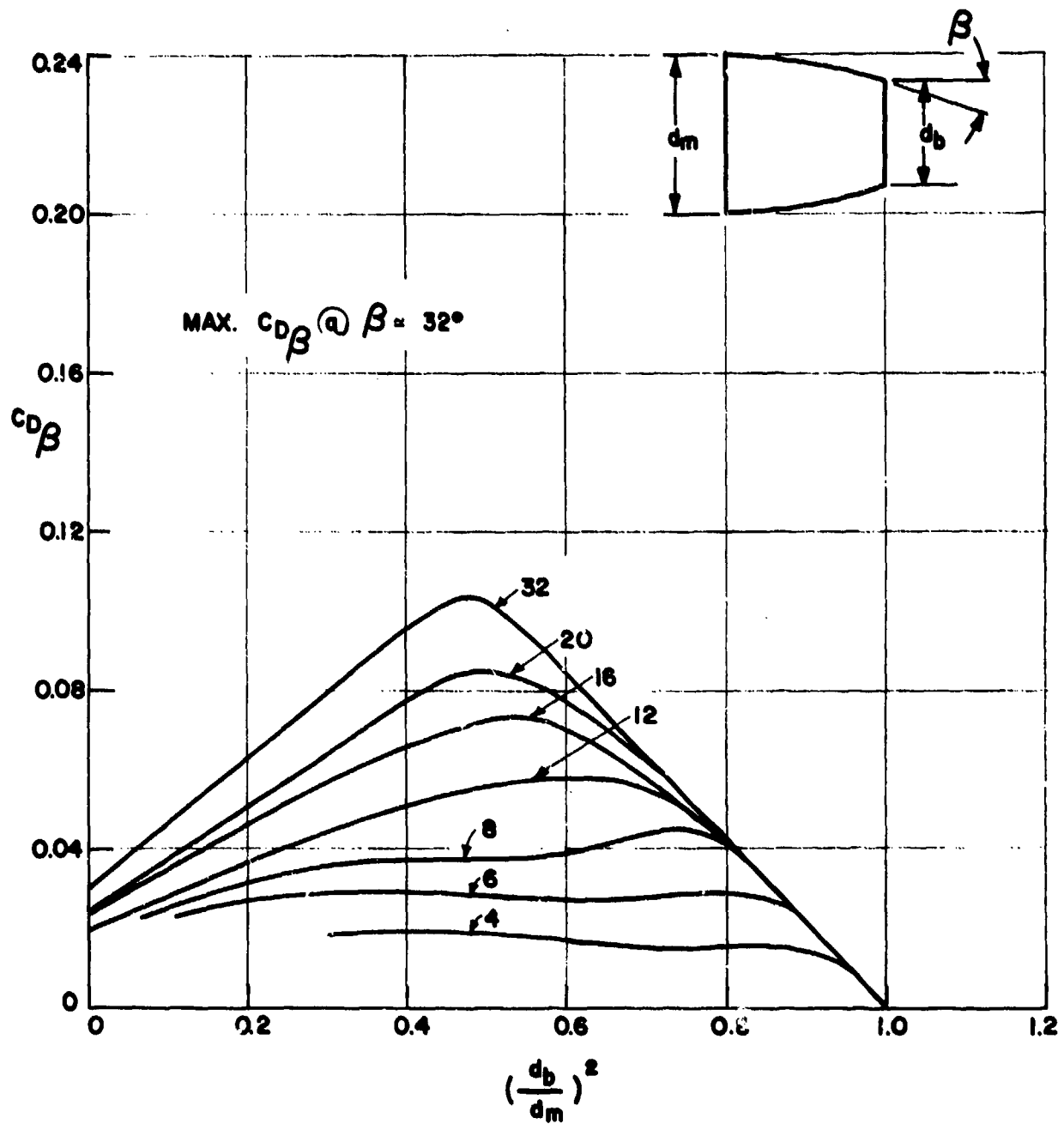


Figure 8a - $M = 0.9$

Figure 8 - Continued

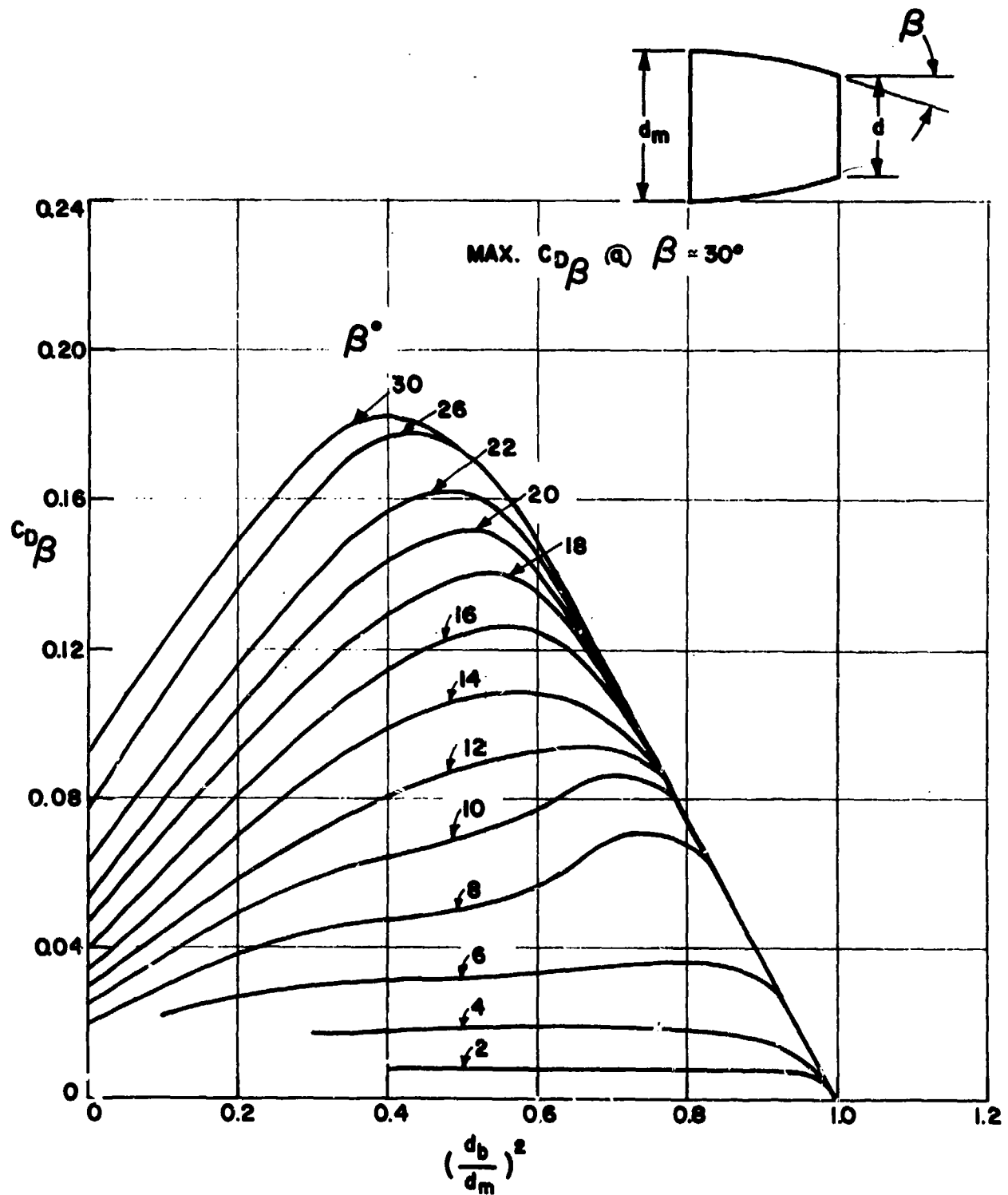


Figure 8d - $M = 1.0$

Figure 8 - Continued

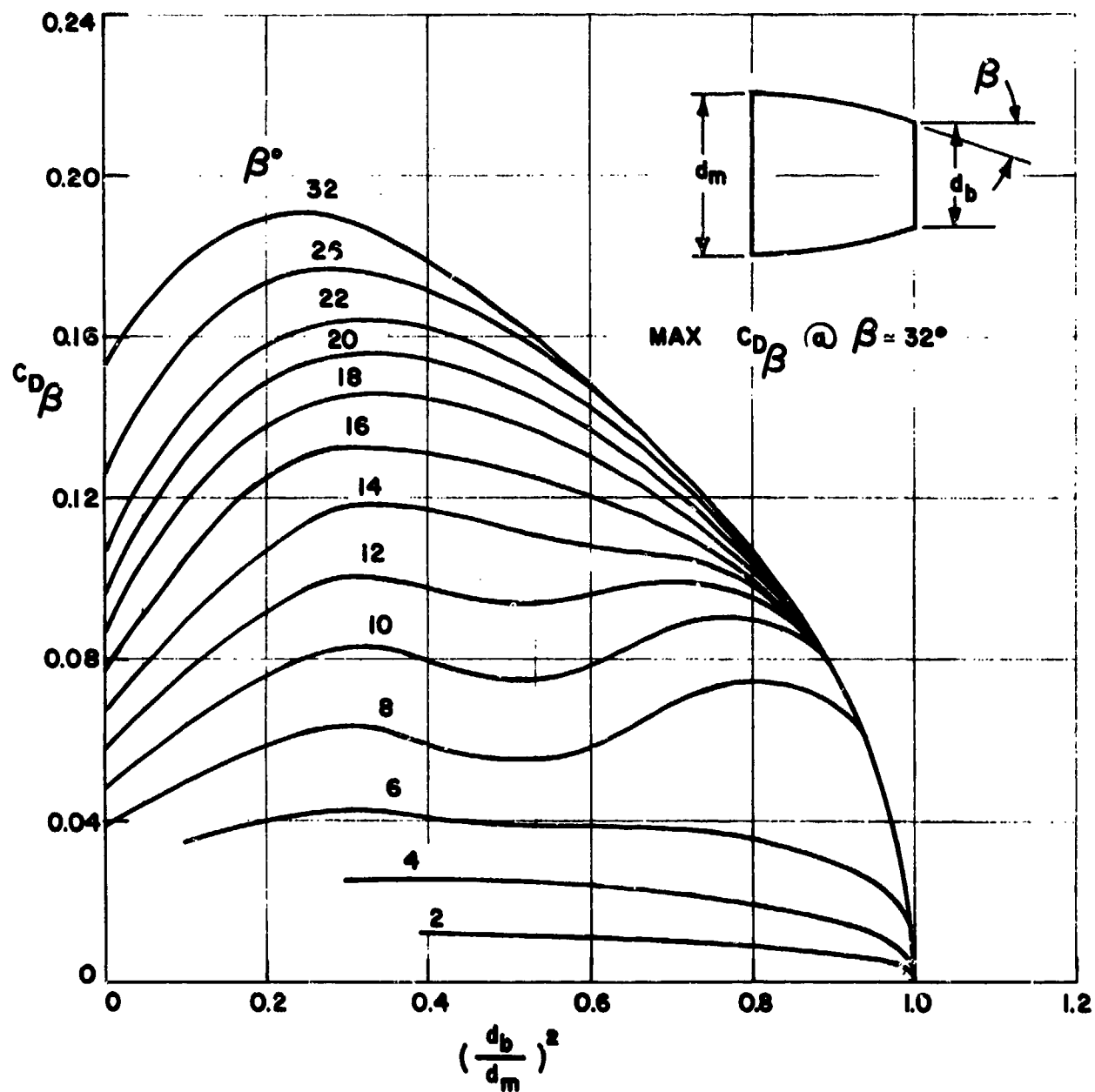


Figure 8e - M = 1.1

Figure 8 - Continued

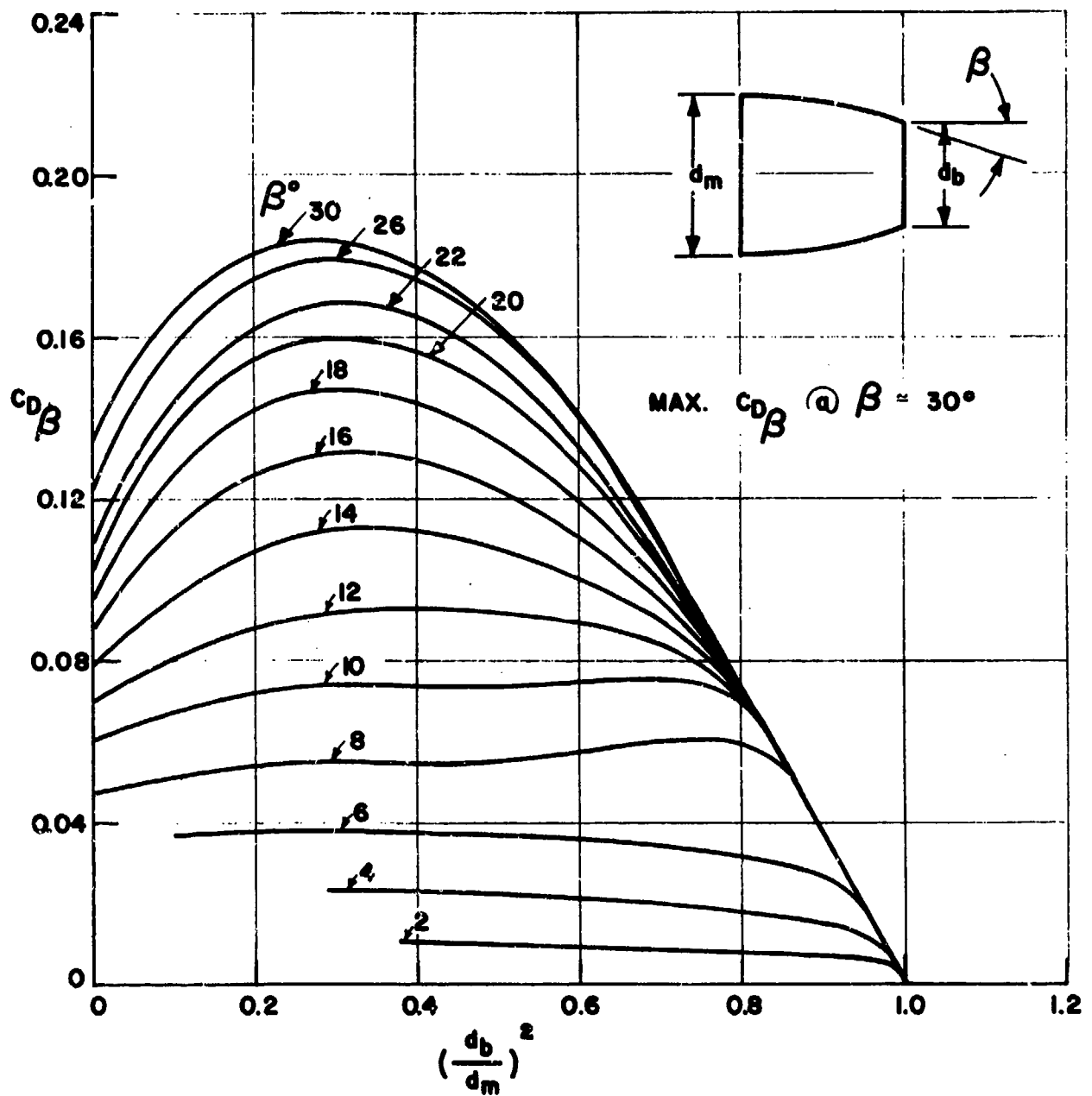


Figure {f - M = 1.2

Figure 8 - Continued

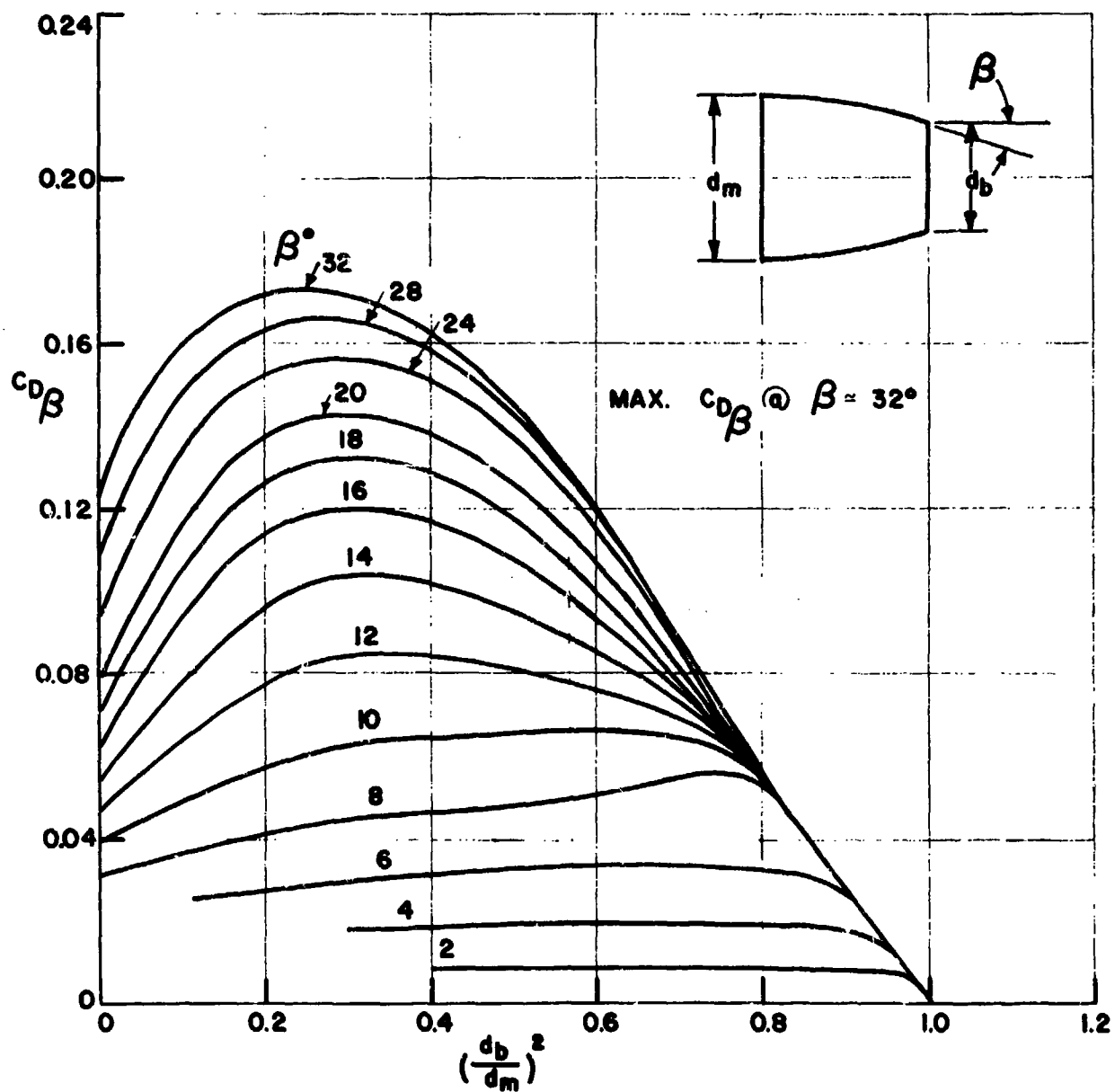


Figure 8g - M = 1.3

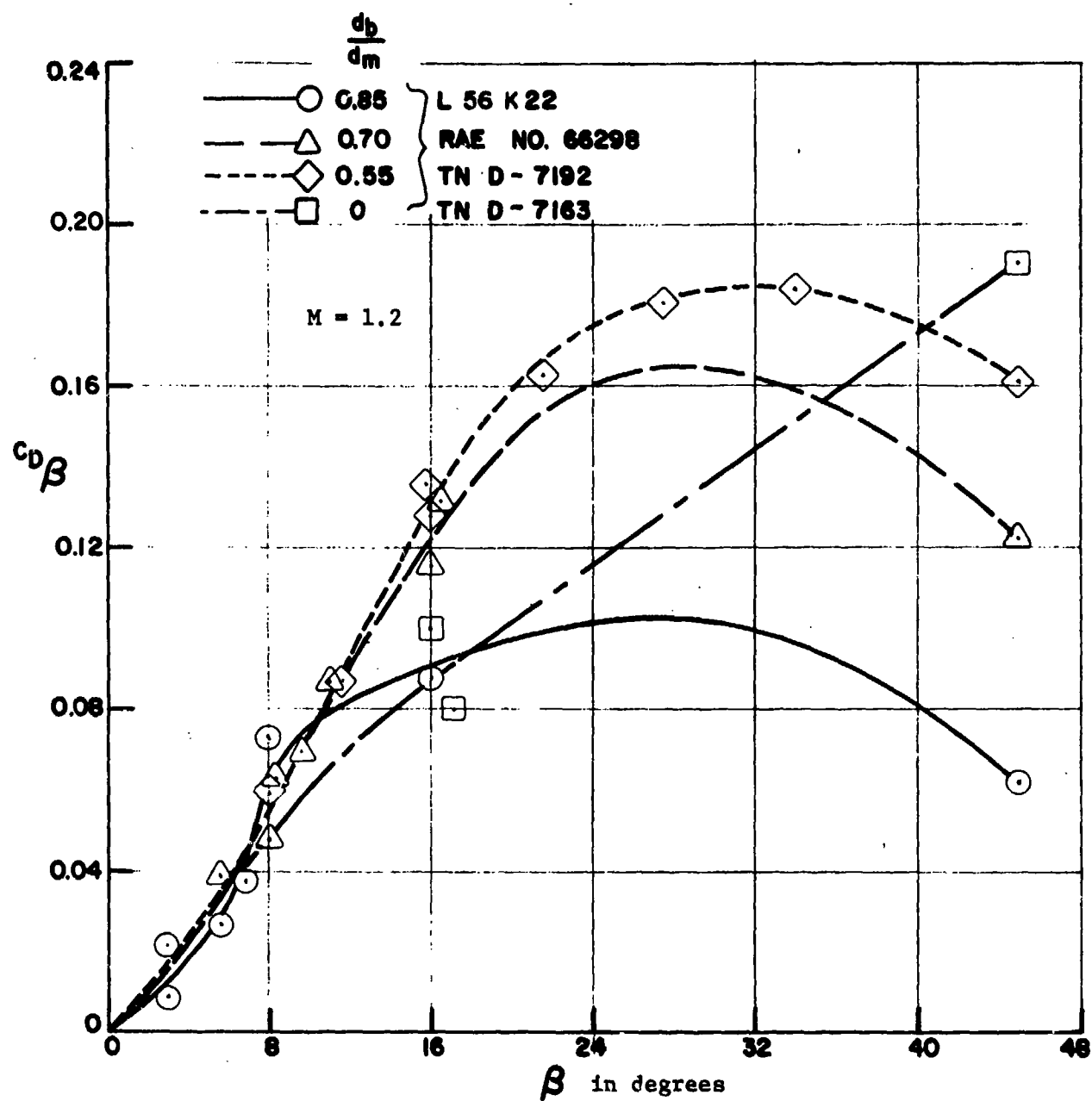


Figure 9 - A Correlation of Circular Arc Boattail Coefficients with Jet Off

Figure 10 - Circular Arc Boattail Base Pressure Coefficients with Jet Off

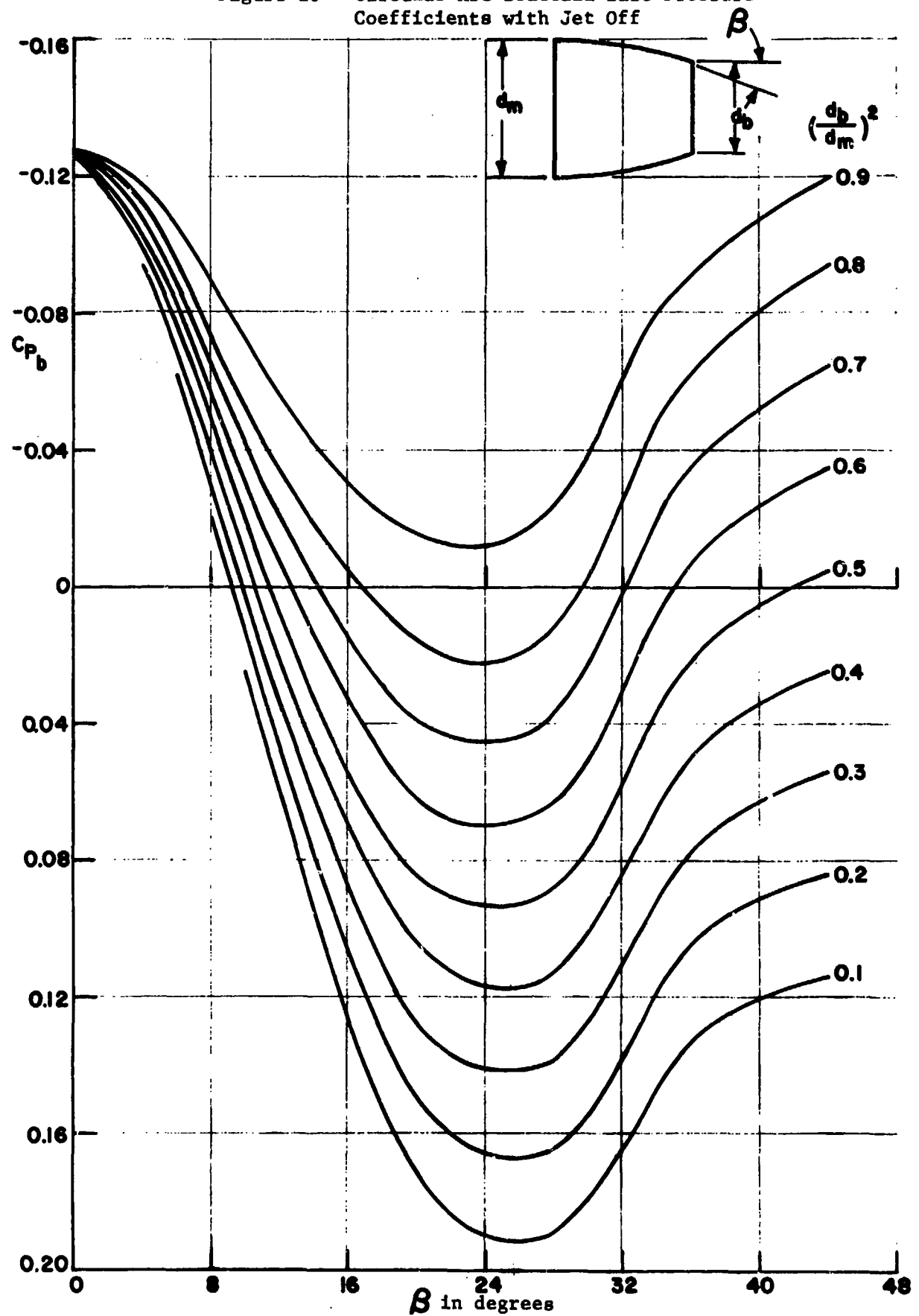


Figure 10a - $M = 0.6$

Figure 10 - Continued

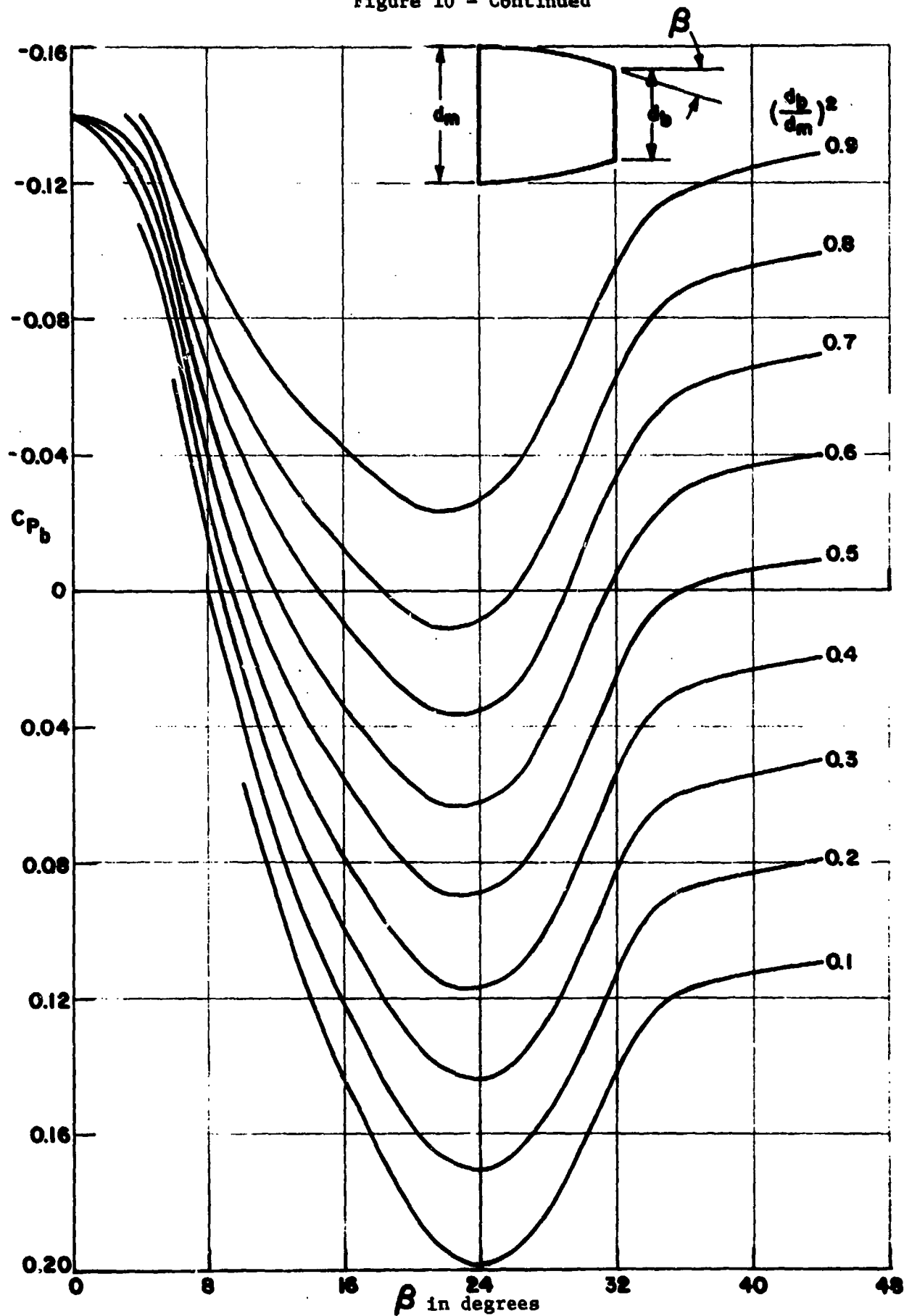


Figure 10b - $M = 0.8$

Figure 10 - Continued

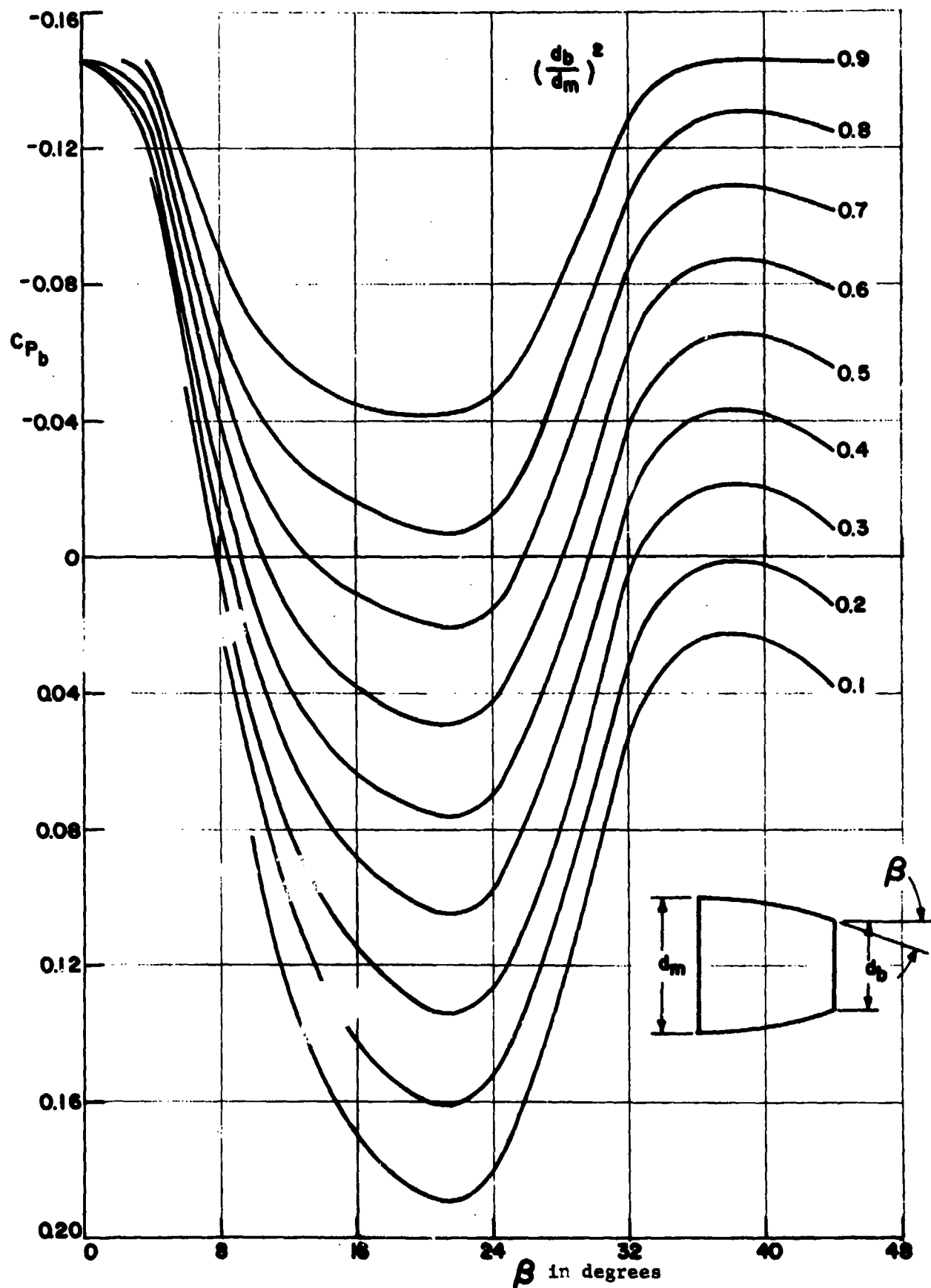


Figure 10c - $M = 0.9$

Figure 10 - Continued

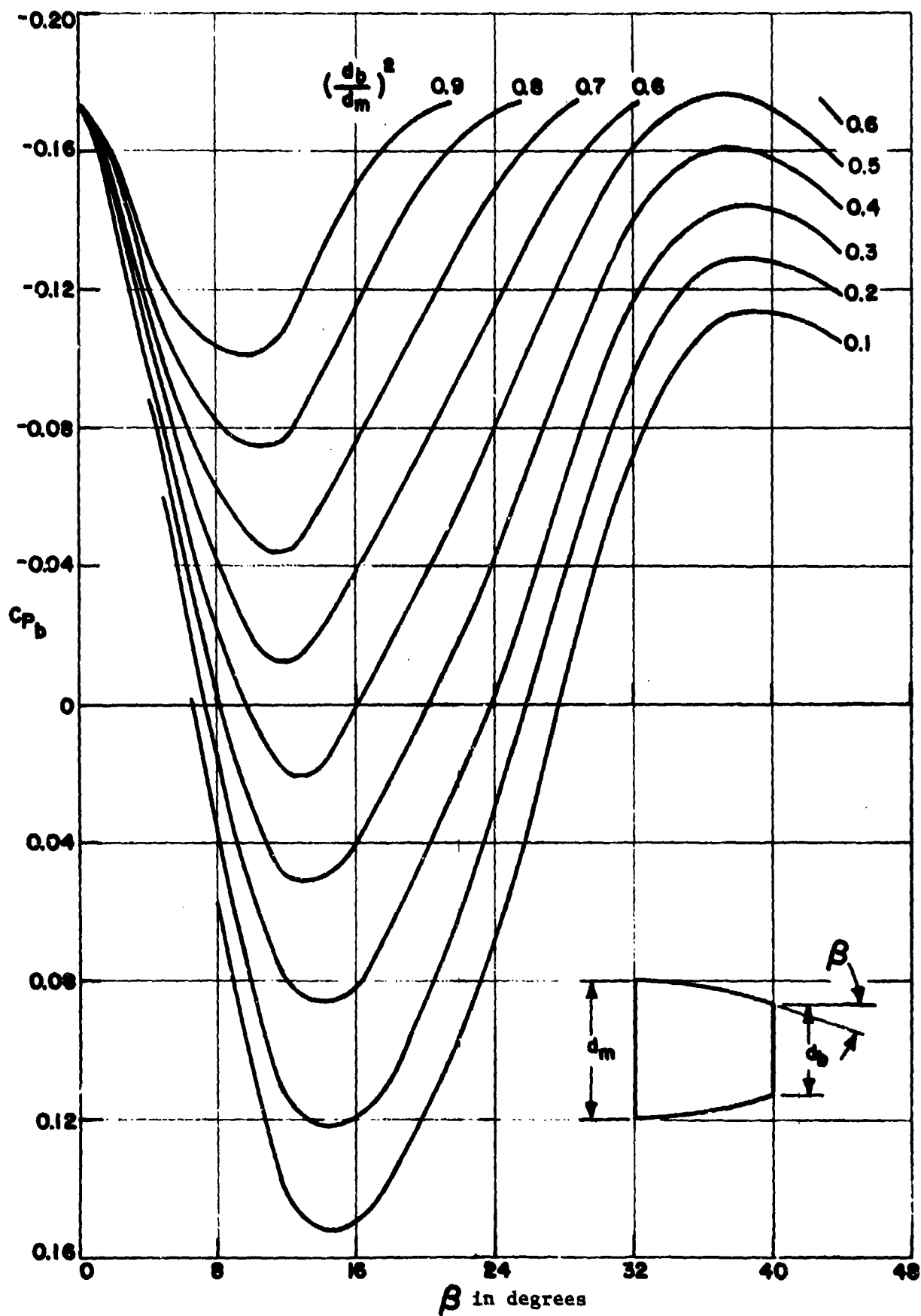


Figure 10d - $M = 1.0$

Figure 10 - Continued

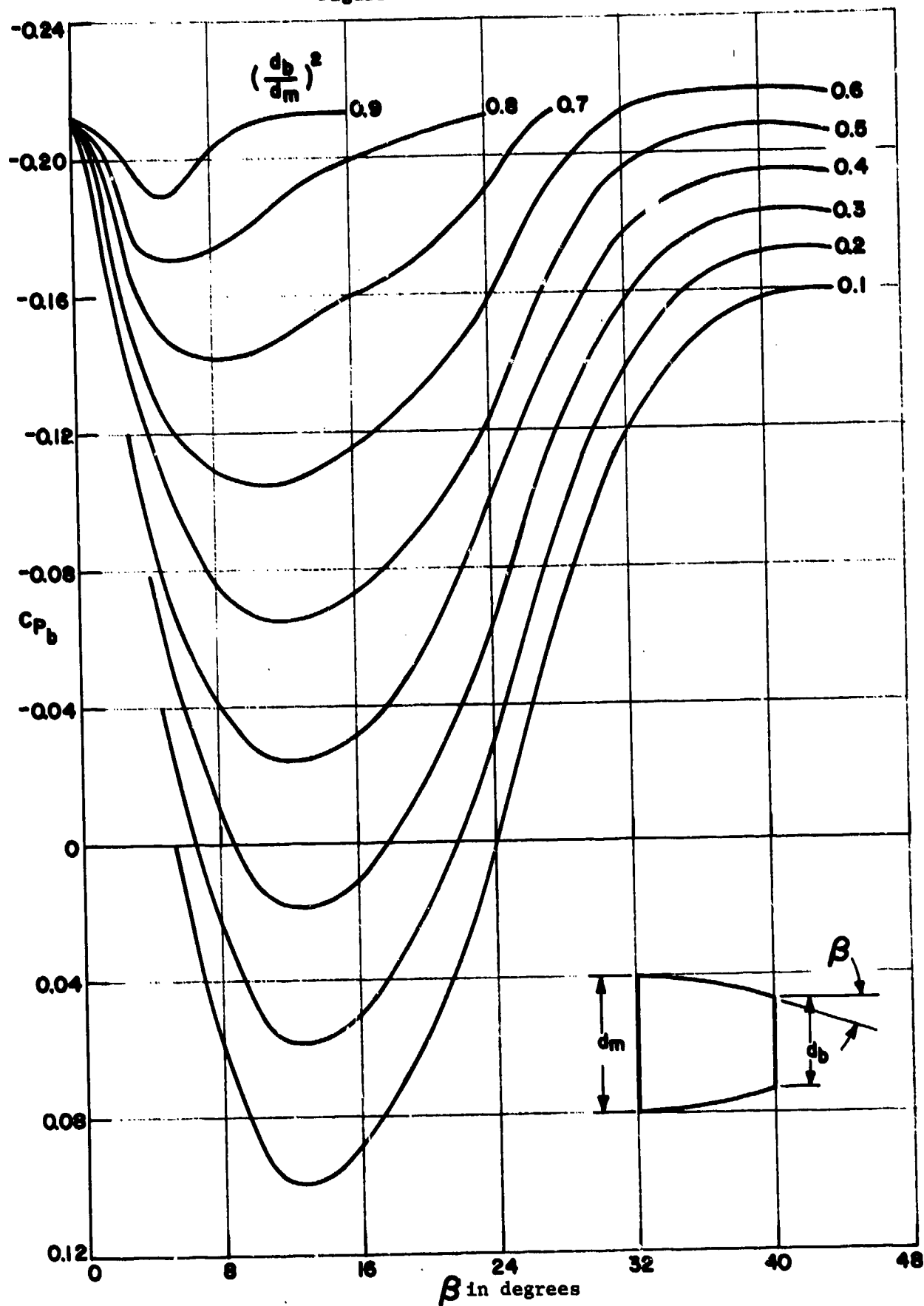


Figure 10e - $M = 1.1$

Figure 10 - Continued

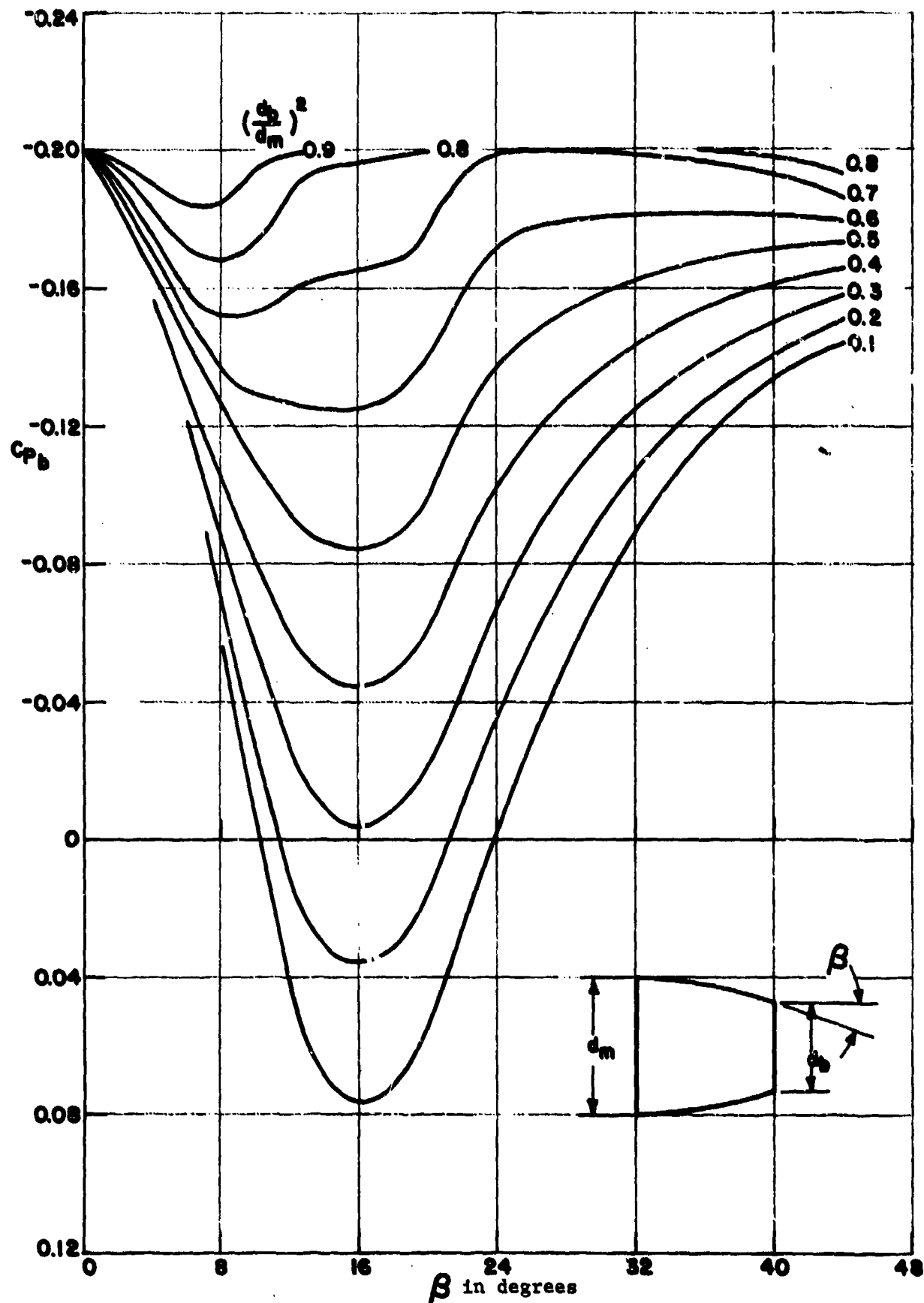


Figure 10f - M = 1.2

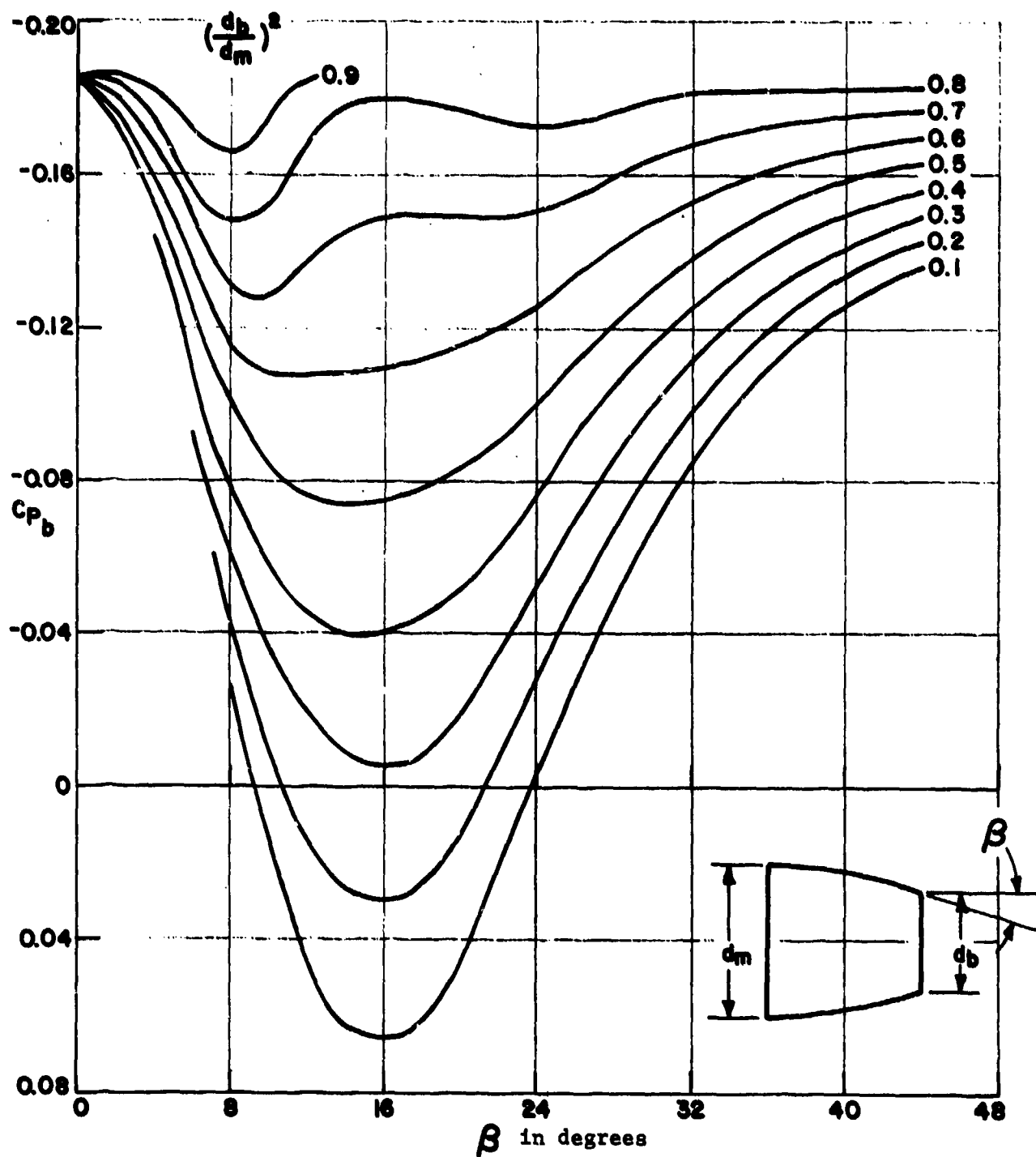


Figure 10g - $M = 1.3$

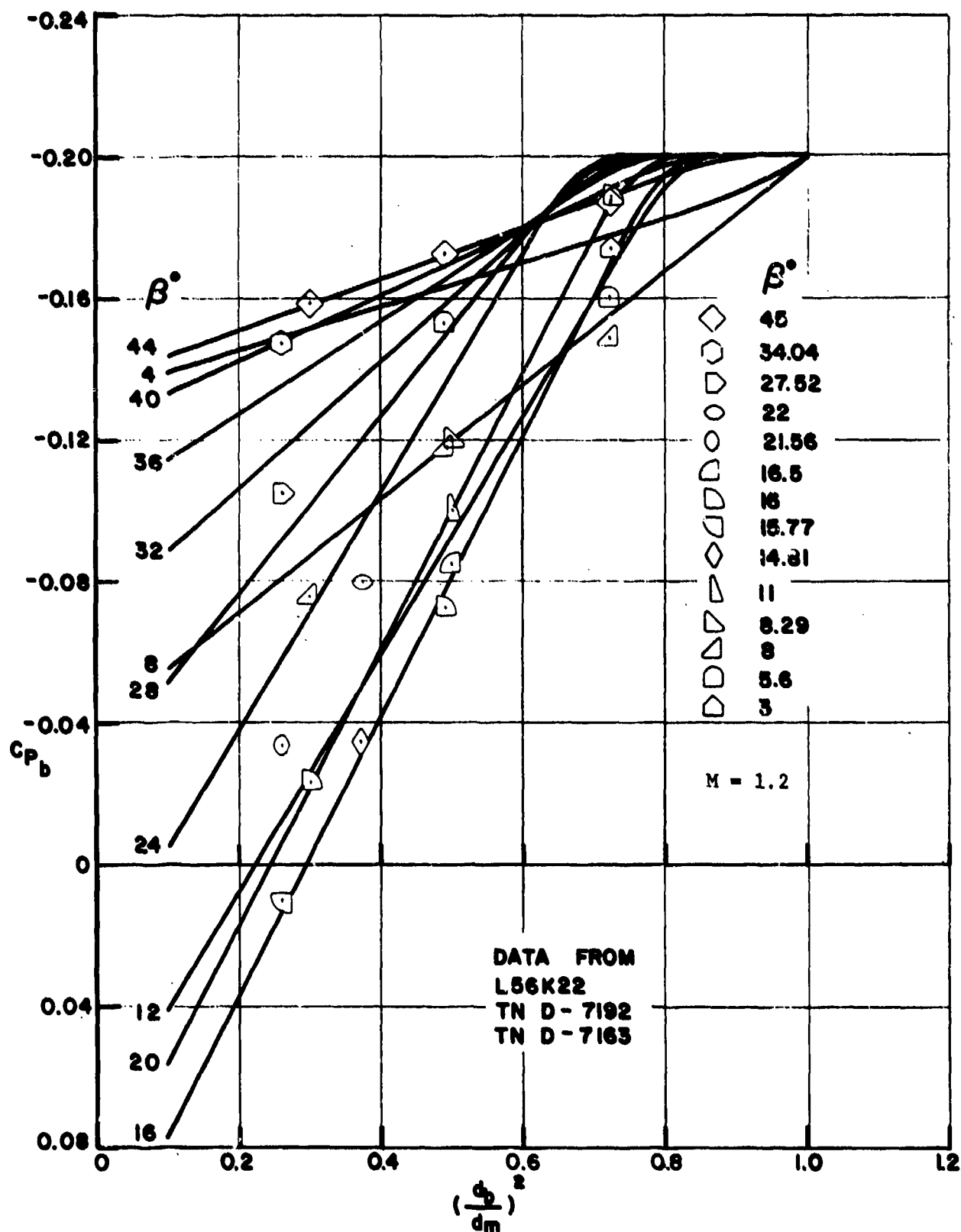


Figure 11 - A Correlation of Circular Arc Boattail Base Pressure Coefficients as a Function of Base Diameter Ratio with Jet Off

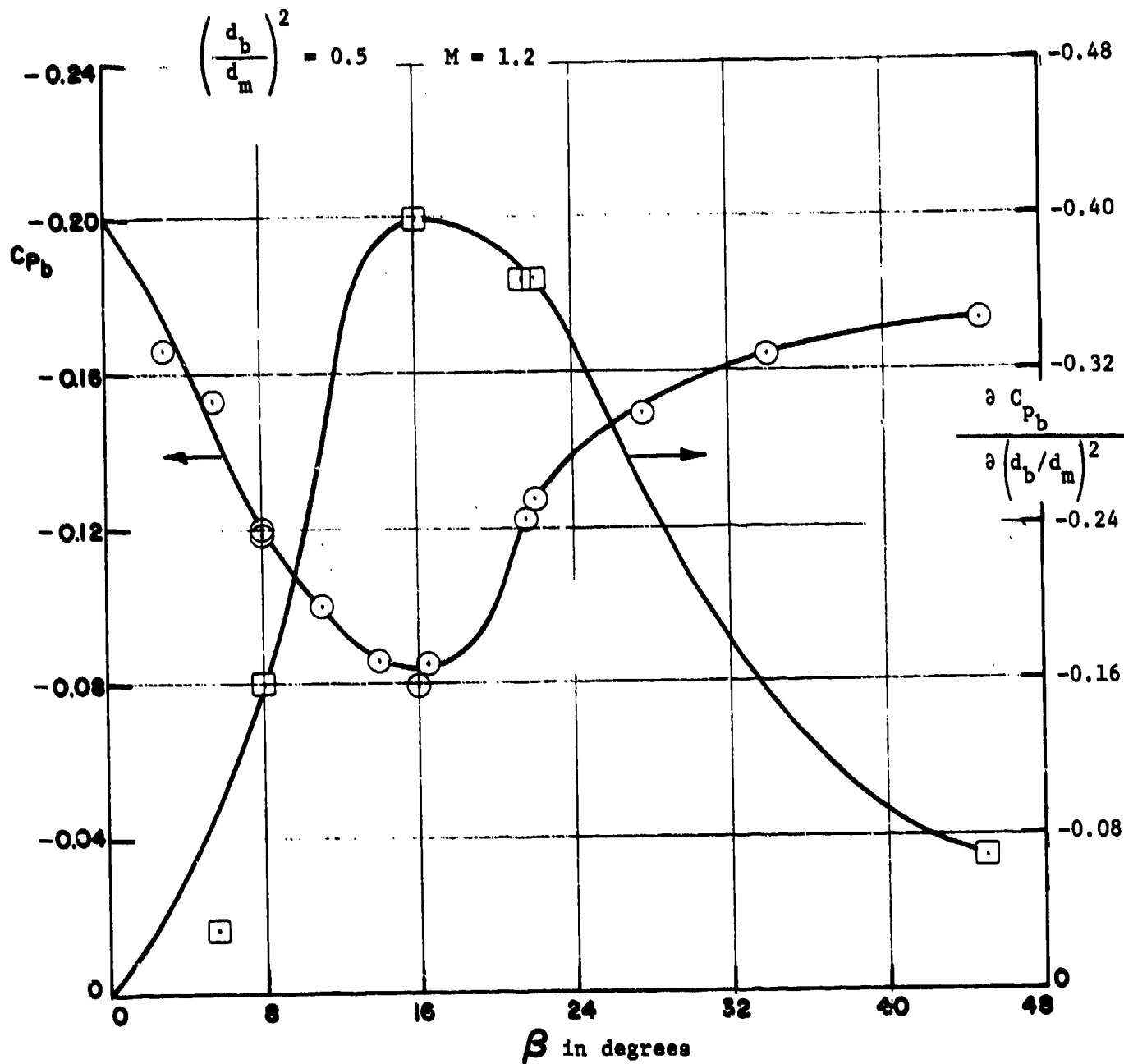


Figure 12 - A Correlation of Circular Arc Boattail
 Base Pressure Coefficients as a Function of
 Boattail Angle with Jet Off

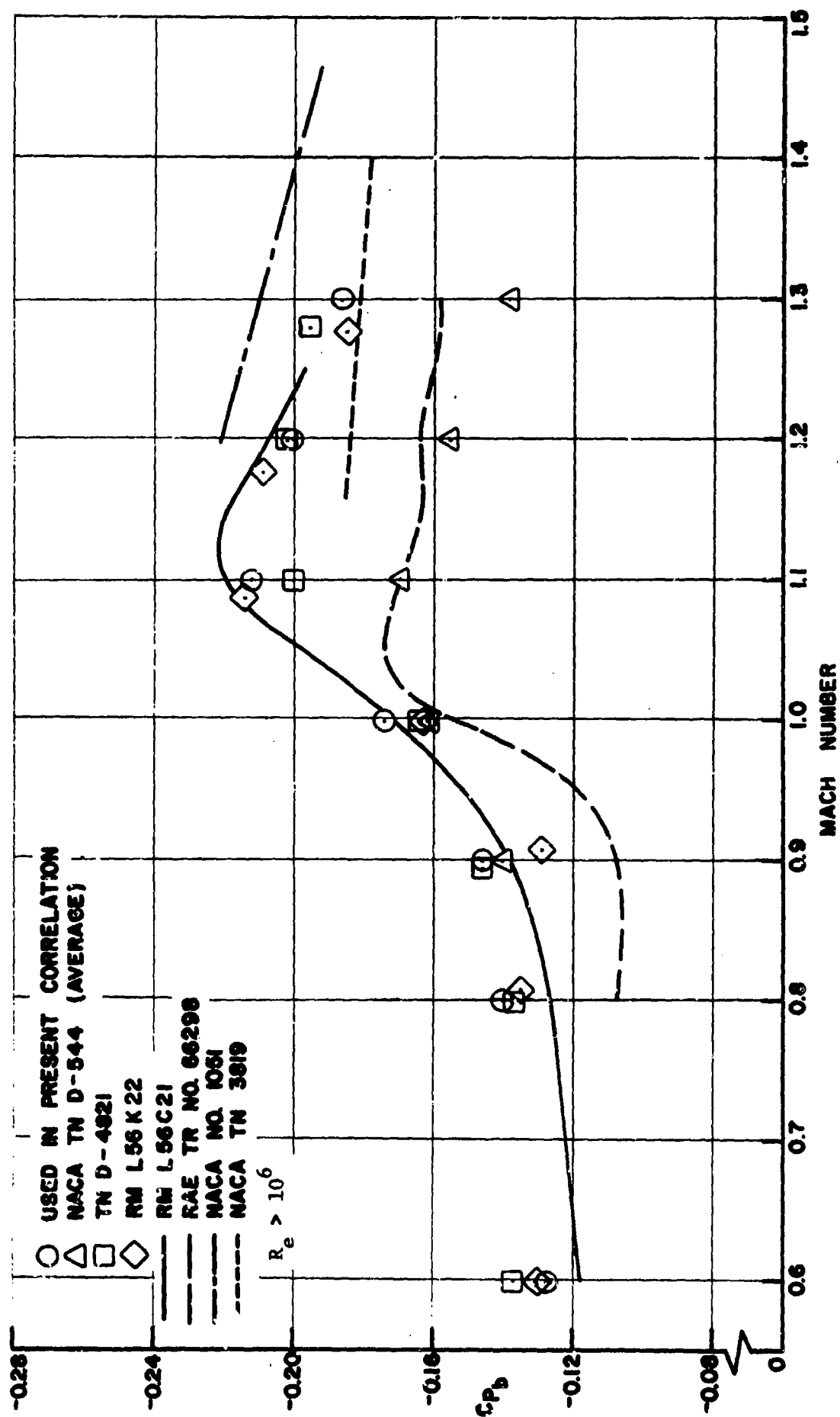


Figure 13 - Cylindrical Afterbody Base Pressure Coefficients with Turbulent Boundary Layer

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